

# Tools and Best Practices for Teaching Higher Level Mathematics

**Sponsored by:**

National Organization of Parents of Blind Children  
Division (NOPBC)

NFB Convention  
ORLANDO, FLORIDA  
July 3, 2018

Presented by  
Susan A. Osterhaus

Texas School for the Blind and Visually  
Impaired

Outreach Programs

1100 West 45th Street

Austin, TX 78756 U.S.A.

[susanosterhaus@tsbvi.edu](mailto:susanosterhaus@tsbvi.edu)

[www.tsbvi.edu/math](http://www.tsbvi.edu/math)

[www.tsbvi.edu/videos-webinars/mathematics](http://www.tsbvi.edu/videos-webinars/mathematics)

# Agenda

- Math Materials (Including Graphics)
  - Blind Learner
  - Low Vision Learner
  - Auditory Learner
- Accessible Math Tools and Technology
  - Basic
  - Number and Quantity
  - Measurement
  - Algebra and Statistics and Probability
  - Geometry

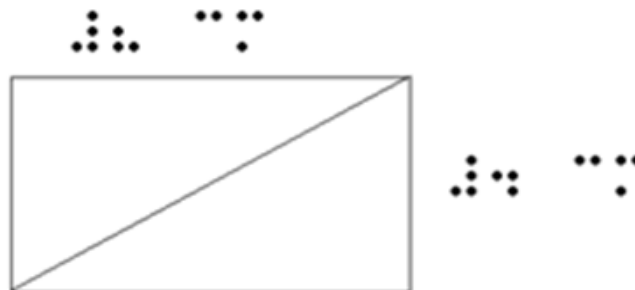
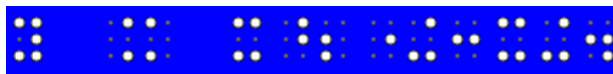
# The Learning of Mathematics

- Highest level of math achieved in high school was shown to be linked with successful completion of a college degree in any field of study (Adelman, 1999 and Hill, 2006)
- **higher level of high school math = higher likelihood of completing college degree**

# Math Materials

## Braille Reader

- High Quality Braille Textbooks & Assessments (including released tests)
  - Nemeth Code
  - Tactile Graphics
- Teacher-Made Materials
  - Worksheets
  - Quizzes
  - Tests



# Nemeth Translation Packages

- Duxbury:  $\geq$  DBT WIN 10.3

[www.duxburysystems.com](http://www.duxburysystems.com)



- MacKichan: Scientific Notebook

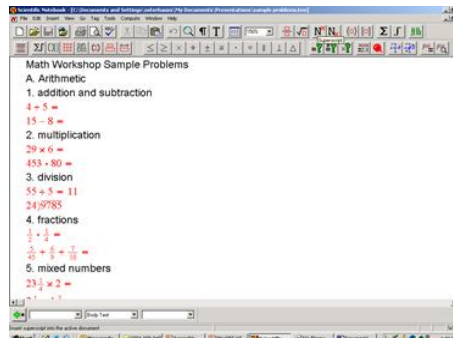
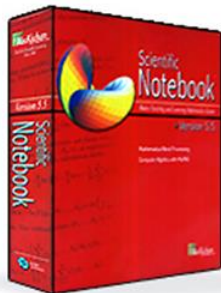
[www.mackichan.com](http://www.mackichan.com)



**Design  
Science**

- Design Science: MathType

[www.dessci.com](http://www.dessci.com)



# Nemeth to Print Back Translators

- Humanware KeySoft 9.5 Upgrade for the BrailleNote Apex  
[http://support.humanware.com/en-usa/support/brailnote\\_apex/software/keysoft\\_95\\_4](http://support.humanware.com/en-usa/support/brailnote_apex/software/keysoft_95_4)  
Humanware Key Math with the Braille Note Touch  
[http://support.humanware.com/en-usa/support/brailnote\\_touch/video\\_tutorials#a15](http://support.humanware.com/en-usa/support/brailnote_touch/video_tutorials#a15)
- Braille Sense Notetaker v8.6 Firmware Update with BookShare fix, new Tablet Viewer feature and Math Symbol Select.  
<https://www.hims-inc.com/news/?mod=document&uid=128>
- Duxbury Systems [www.duxburysystems.com](http://www.duxburysystems.com)  
Now Translating from Braille Math to Inkprint Math via Word\*  
\*Requires Microsoft Word and MathType

# Bristol Braille Canute: Multi-line Refreshable Braille

<http://www.bristolbraille.co.uk/>

- The *Canute 360* is a nine line, 360-cell standalone braille e-reader.
- Entering final testing period with release later in 2018
- Single line braille displays and talking books can never fully replace braille in the STEM fields.



Understanding in these subjects requires information to be rendered *in context*: math problems, data tables, equations, etc. require information to be presented over a series of lines, not a single line of text.

# Resources for Learning Nemeth Code

- **Publications Available to Learn Nemeth Code**  
[www.tsbvi.edu/component/content/article/1523-publications-available-to-learn-nemeth-code](http://www.tsbvi.edu/component/content/article/1523-publications-available-to-learn-nemeth-code)
- **Other Ways to Learn Nemeth Code**  
[www.tsbvi.edu/component/content/article/1522-other-ways-to-learn-nemeth-code](http://www.tsbvi.edu/component/content/article/1522-other-ways-to-learn-nemeth-code)
- **Nemeth Code Reference Sheets**  
[www.tsbvi.edu/resources-math/1524-nemeth-code-reference-sheets](http://www.tsbvi.edu/resources-math/1524-nemeth-code-reference-sheets)
- **Nemeth Updates**  
[www.brailleauthority.org/mathscience/math-science.html](http://www.brailleauthority.org/mathscience/math-science.html)

# What's New with Learning Nemeth!

- *Guidance for Transcription Using the Nemeth Code within UEB Context*,  
Approved June 2016 (Revised 2018)  
[www.brailleauthority.org/mathscience/math-science.html](http://www.brailleauthority.org/mathscience/math-science.html)
- *Nemeth at a Glance: A Math Resource, Grade Level Chart, and Evaluation Tool*  
[www.tsbvi.edu/store/ecom/index.php?action=ecom.pdetails&mode=nemeth](http://www.tsbvi.edu/store/ecom/index.php?action=ecom.pdetails&mode=nemeth)

# Online Nemeth

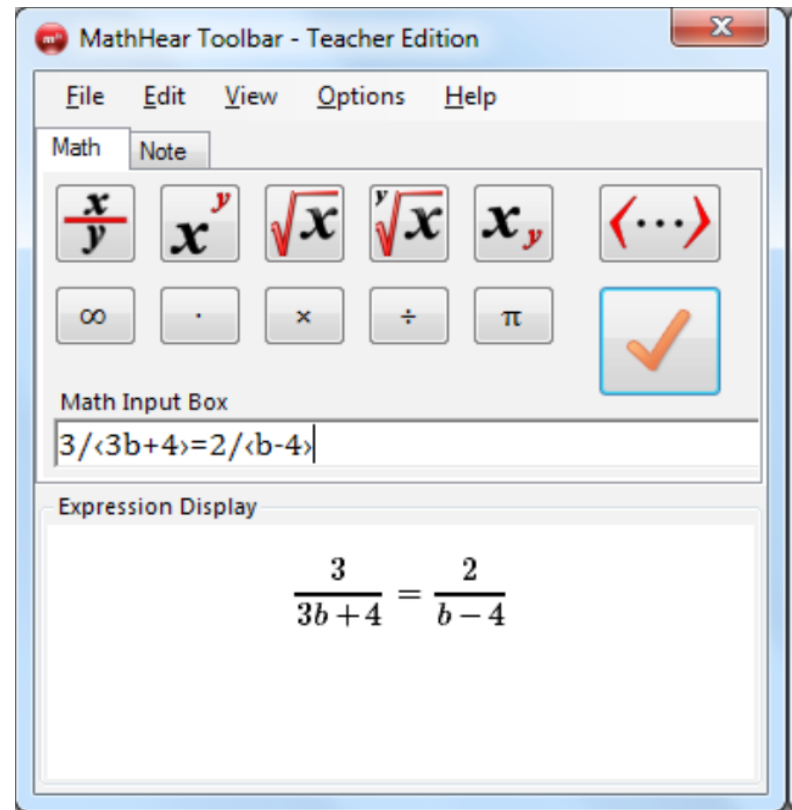
- APH Nemeth Tutorial  
<https://tech.aph.org/nemeth/>
- Nemeth Braille Searchable Database  
<http://accessibility.pearson.com/nemethdatabase>
- TSBVI Online Nemeth Tutorial (coming soon)

# MathHear for Windows



[www.gh-accessibility.com/software/mathhear](http://www.gh-accessibility.com/software/mathhear)

- MathHear provides simple and accurate math access to teachers and students via a keyboard-accessible interface. Full voicing provides blind and visually impaired users with complete access to both basic and advanced math expressions, enabling all students to participate equally in online learning activities.



# Math Speech and Braille Display

- Math Player + MathType + NVDA

[www.dessci.com/en/reference/ies-ets/instructional\\_material/default.htm#navigation\\_guide](http://www.dessci.com/en/reference/ies-ets/instructional_material/default.htm#navigation_guide)

- JAWS

[www.freedomscientific.com/JAWSHQ/JAWSHeadquarters01](http://www.freedomscientific.com/JAWSHQ/JAWSHeadquarters01)

[www.freedomscientific.com/content/html/jawshq/MathML-Samples.html](http://www.freedomscientific.com/content/html/jawshq/MathML-Samples.html)

[http://podcast.freedomscientific.com/FSCast/episodes/FSCast128-Conference\\_Specials,MathML,Mike\\_Wood.mp3](http://podcast.freedomscientific.com/FSCast/episodes/FSCast128-Conference_Specials,MathML,Mike_Wood.mp3)

# Accessible Equation Editor

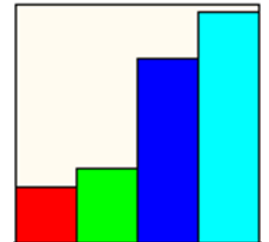
<http://accessibility.pearson.com/mathex-app/>

The image shows the interface of the Accessible Equation Editor. At the top is a toolbar with icons for basic arithmetic (+, -, ×, ÷), fractions, powers ( $y^x$ ), square roots ( $\sqrt{\quad}$ ), equals (=), approximate (≈), undo, redo, delete, and a clear button. Below the toolbar is a large text area where the equation  $x^2 + y^2 = 4$  has been entered. To the right of the text area is a vertical menu with categories: Numbers, Constants, Symbols, Arithmetic, Fractions, Groups, Relations, Radicals, Scripts, Functions, Trigonometry, Hyperbolic, and Omissions. At the bottom of the interface is a Braille display showing the Braille representation of the equation  $x^2 + y^2 = 4$ .

# Math Materials

## Large Print Reader

- Large Print Textbook
- Enlarged Materials
- Regular Print with Magnification
- Be Alert for Color-Keyed Graphics



# Accessible Math Graphics

- Tactile Graphics
- Large Print Graphics
- Universally Designed Math Graphics for both the Student Who is Blind or Who Has Low Vision

# *Guidelines and Standards for Tactile Graphics, 2010*

from the Braille Authority of North America  
(BANA) and Canadian Braille Authority (CBA)

[www.brailleauthority.org/](http://www.brailleauthority.org/)

Available for purchase from APH...

Print: 7-35935-00      Braille: 5-35935-00

# *Guidelines and Standards for Tactile Graphics*

## *Supplement: Examples 1 - 35*

The tactile graphics examples illustrated in this supplement have been designed to accompany the *Guidelines and Standards for Tactile Graphics 2010*. Each tactile graphic is preceded by a brief summary of the important design techniques and braille formats used in each example.

Available for purchase from APH...

Print: 7-35936-00

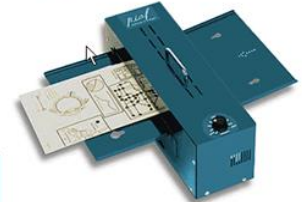
Braille: 5-35936-00

# Tactile Imaging Machine and Swell Touch Paper

- Pictures in a Flash (PIAF)  
[www.humanware.com](http://www.humanware.com)

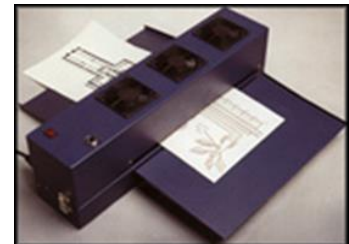
PIAF - Pictures In A Flash

Tactile graphics made 1-2-3 easy!



A Simple and Fast Way to Produce Tactile Graphics

- Swell-Form Graphics Machine  
[www.americanthermoform.com](http://www.americanthermoform.com)



# ViewPlus Braille Embossers are all Powered by Tiger®



[www.viewplus.com](http://www.viewplus.com)



- **Braille production made flexible and easy:**  
Braille is translated and embossed from MS Word in one touch and graphics are produced from any PC software including Illustrator & CorelDraw.
- **Braille and Ink:**  
Prints Braille and ink on the same page in a single pass.
- **Tactile graphics embossed in fine detail:**  
Tiger tactile graphics are the highest-resolution of any embosser.
- **Braille & graphics software included:**  
TSS incorporates braille software, tactile graphic studio, and more. It is also compatible with Duxbury and other braille software.

# Phoenix Braille and Tactile Graphics Embosser

<http://brailleur.com/products/phoenix>



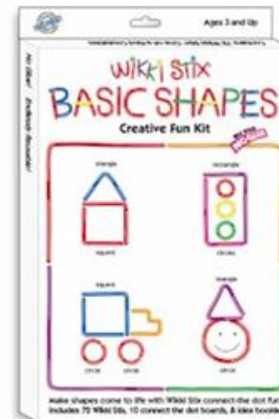
- Introducing Phoenix, the World's first multi-function Braille and Tactile Graphics System.
- Imagine the ability to scan your pictures, graphs and charts into your computer and with a few clicks of the mouse, emboss those images in high definition tactile graphics without compromising the quality of your Braille text.

# Quick/Instant Tactile Graphics

- APH Picture Maker:  
Wheatly Tactile  
Diagramming Kit



- WikkiStix  
[www.wikkistix.com](http://www.wikkistix.com)



# More Quick Tactile Graphics

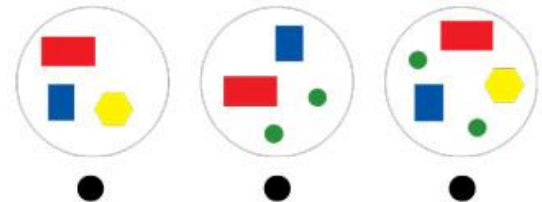
- APH Draftsman
- E.A.S.Y. inTACT Sketchpad
- Sewell Raised Line Drawing Board
- Sensational Blackboard



# TTT: Talking Tactile Tablet



3



- [www.touchgraphics.com](http://www.touchgraphics.com)

TTT Math

# TTP: Talking Tactile Pen



- [www.touchgraphics.com](http://www.touchgraphics.com)

# IVEO® Touchpad



- [www.viewplus.com](http://www.viewplus.com)

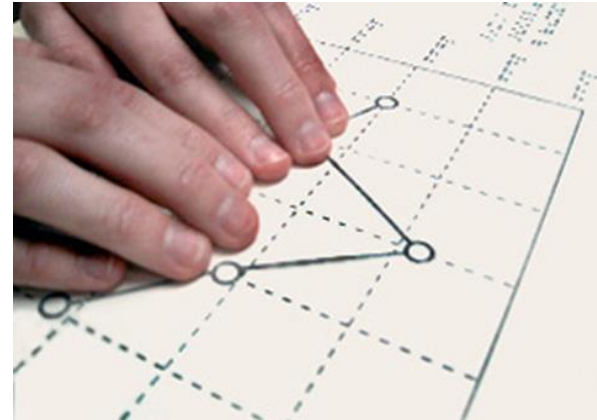


# Math Graphics Made to Order by Others

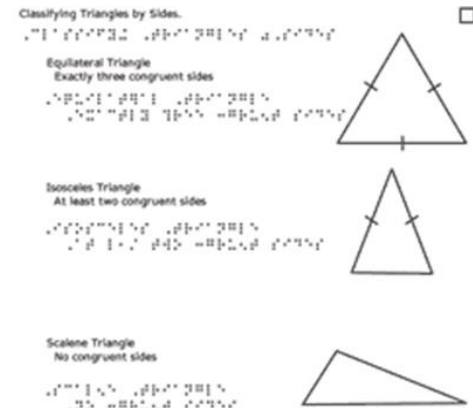
- gh, LLC

LaserLine™ Graphics

[www.gh-accessibility.com](http://www.gh-accessibility.com)

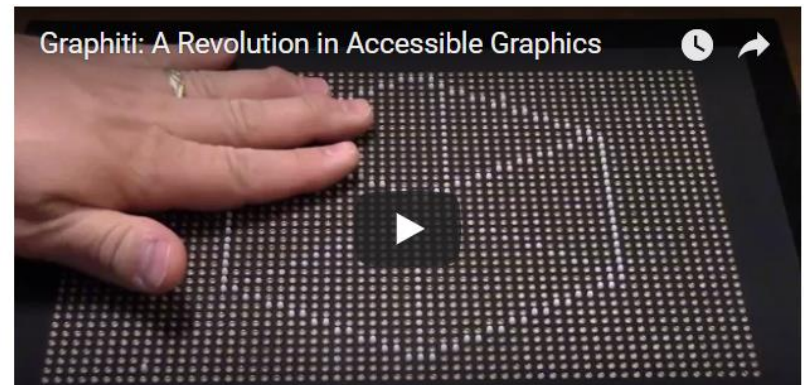


- Tactile Vision Graphics  
<http://tactilevisiongraphics.com>



# Graphiti [www.aph.org](http://www.aph.org)

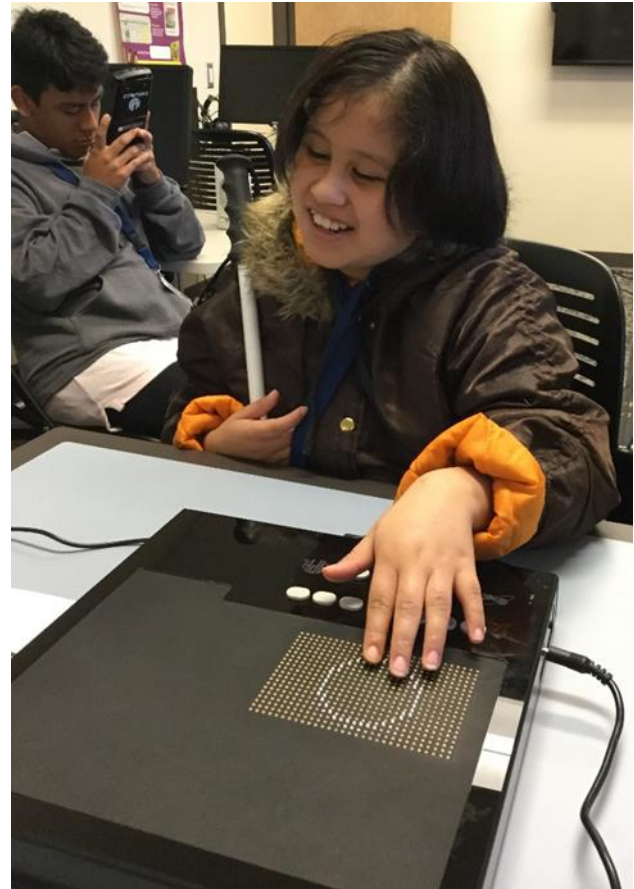
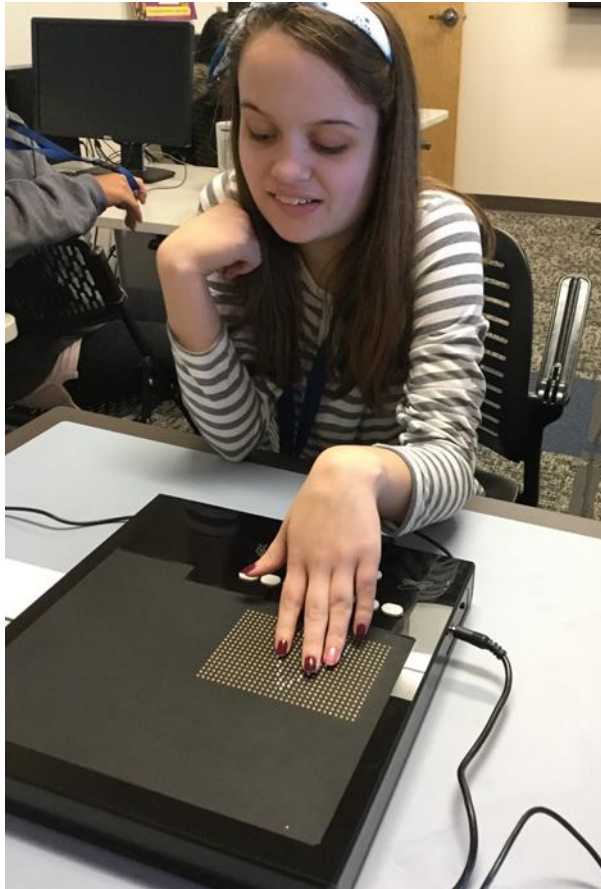
- **Graphiti is a dynamic multilevel tactile touch display** developed by [Orbit Research](http://OrbitResearch.com) and the American Printing House for the Blind. Graphiti allows students and adults to access a wide variety of on-screen graphics by touch.



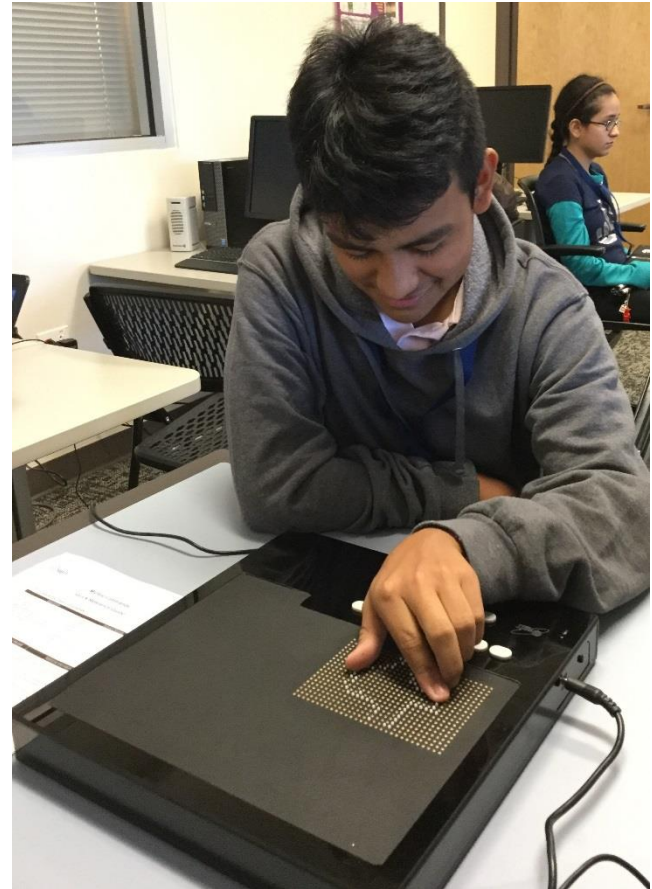
# Graphiti – Short Term Programs' Math Tools Class - Guess the Shape



# Graphiti – Triangle and Circle



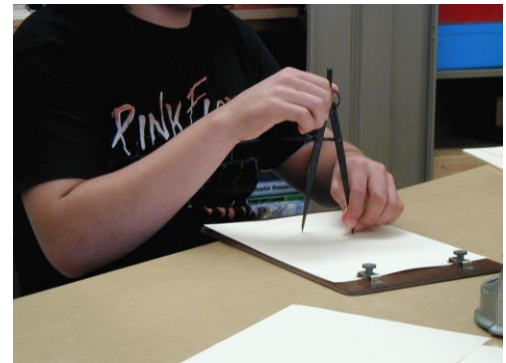
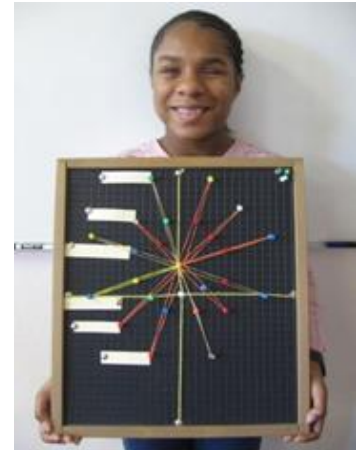
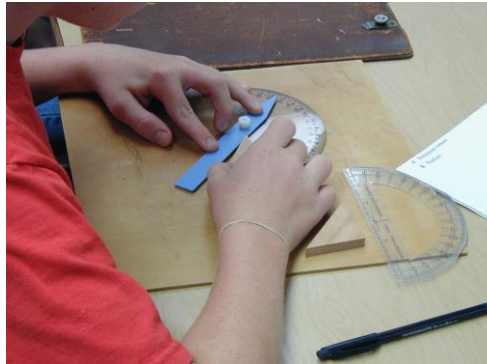
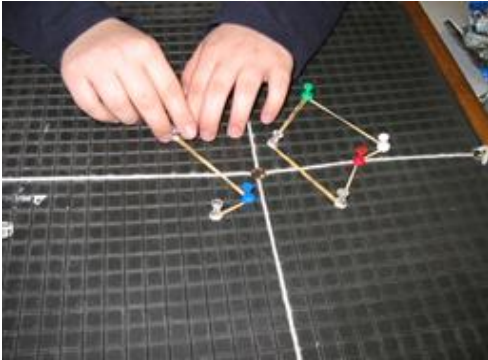
# Graphiti – Is that Texas?



# Graphiti with the Orion TI-84+ Talking Graphing Calculator



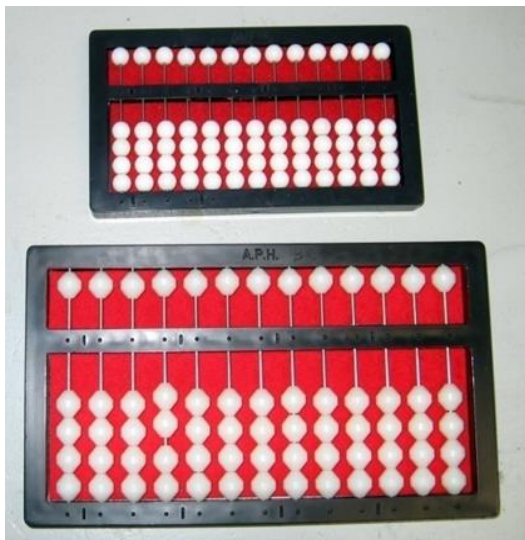
# Accessible Math Tools and Technology



# Number and Quantity

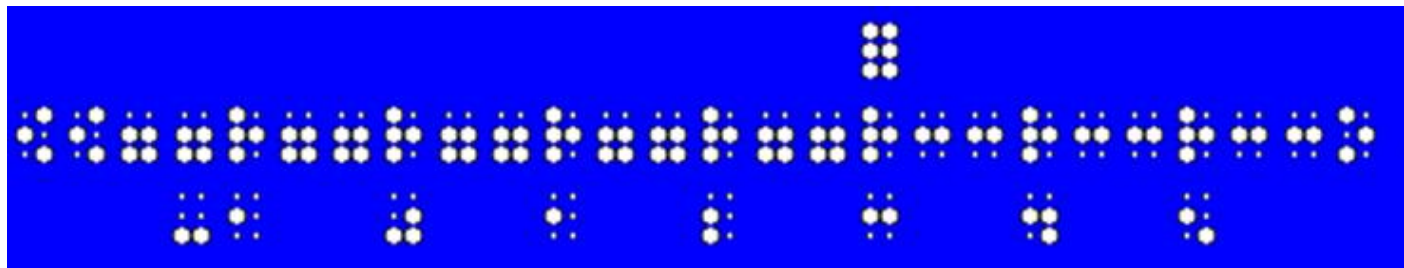
# Abaci from APH [www.aph.org](http://www.aph.org)

- Cranmer Abacus



# Student-Generated Graphics on a Number Line

- APH Number Line Device
- APH Consumable Number Lines
- Desktop Stick-On Number Lines
- Student-Made Number Lines



# Publications and Videos

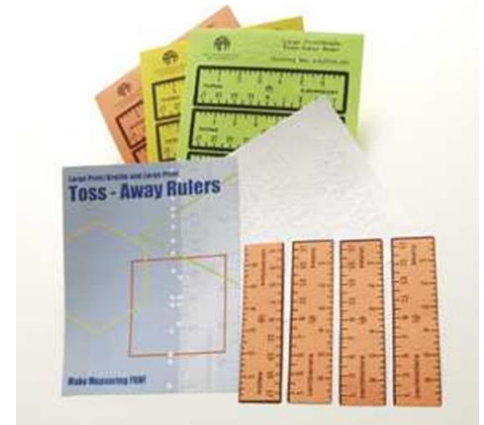
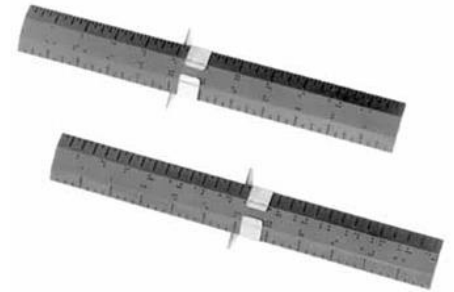
- Prime Factorization on the Abacus  
[www.tsbvi.edu/videos-webinars/mathematics](http://www.tsbvi.edu/videos-webinars/mathematics)
- Osterhaus, S.A. (2003). *Susan's Math Technology Corner: Standardized Braille Number Lines*. *Division on Visual Impairments Quarterly*, 48(2), 9-11  
[www.tsbvi.edu/resources/2316-susans-math-technology-corner-standardized-braille-number-lines](http://www.tsbvi.edu/resources/2316-susans-math-technology-corner-standardized-braille-number-lines)

# Measurement

# Linear and Angle Measurement

[www.tsbvi.edu/tools/2181-math-tools#equipment](http://www.tsbvi.edu/tools/2181-math-tools#equipment)

- Ruler
- Yardstick and Meter Stick
- Toss-Away Rulers
- Protractor

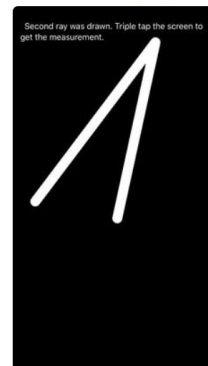


# Draw2Measure Protractor App

<http://www.aph.org/products/mobile-apps/>

- Draw2Measure Protractor App for iOS® devices allows blind and visually impaired students to measure angles in two ways!

First, students can place an angle over the screen of a device, such as a phone or tablet, and trace along the sides of the angle with a fingertip or stylus. The app records the locations of the sides and then calculates the angle.



# Tactile Caliper – 1/16 inch precision

[www.squirreldevices.com](http://www.squirreldevices.com)

[www.youtube.com/watch?v=JOi8zTI9TwY](http://www.youtube.com/watch?v=JOi8zTI9TwY)

- The caliper is accurate to 1/16". There are subtle audible cues when it is operating. The caliper is 12 inches long, the size of a standard ruler. The caliper's design allows for small objects to be inserted into the caliper's opening. This eliminates some common problems for students including holding the ruler steady and lining up the ruler to begin measuring.



The caliper is available from the online store at National Braille Press.

[www.nbp.org/ic/nbp/CALIPER.html](http://www.nbp.org/ic/nbp/CALIPER.html)

# Tactile Caliper – 1 mm Precision

- This metric caliper is brand new and currently being field tested by APH.
- Should be available soon, along with the English measurement tactile caliper, from APH on federal quota funds.



# Temperature



Tactile Demonstration  
Thermometer

[www.aph.org](http://www.aph.org)



Talking Lab Quest

<http://www.independencescience.com>

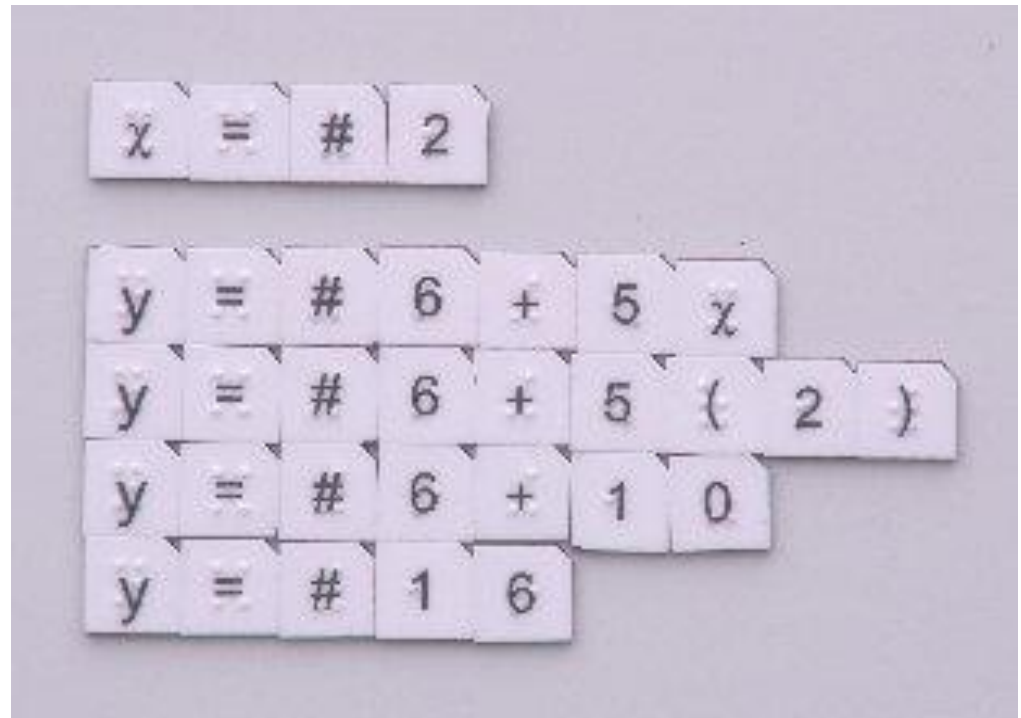
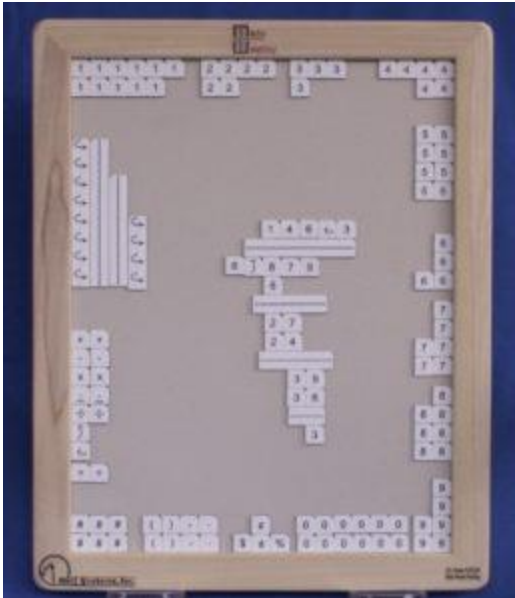
# Measurement Resources

- Linear Measure, Perimeter, Area  
[www.tsbvi.edu/resources-math/3237-teaching-strategies#Linear](http://www.tsbvi.edu/resources-math/3237-teaching-strategies#Linear)
- APH Braille/Print Protractor  
[www.tsbvi.edu/videos-webinars/mathematics](http://www.tsbvi.edu/videos-webinars/mathematics)
- Perkins School for the Blind  
[www.perkinselearning.org/accessible-science](http://www.perkinselearning.org/accessible-science)
- Independence Science  
[www.independencescience.com](http://www.independencescience.com)

# Algebra and Statistics and Probability

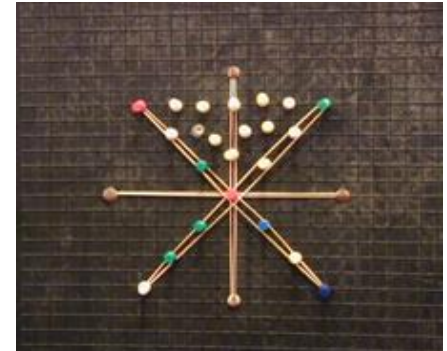
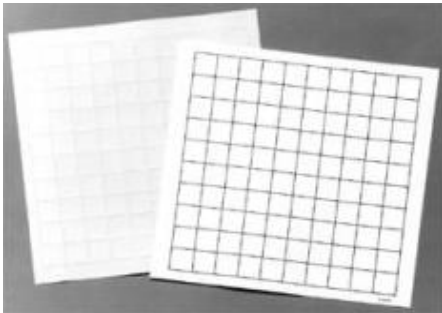
# Math Window Algebra Add-On

[www.mathwindow.com](http://www.mathwindow.com)

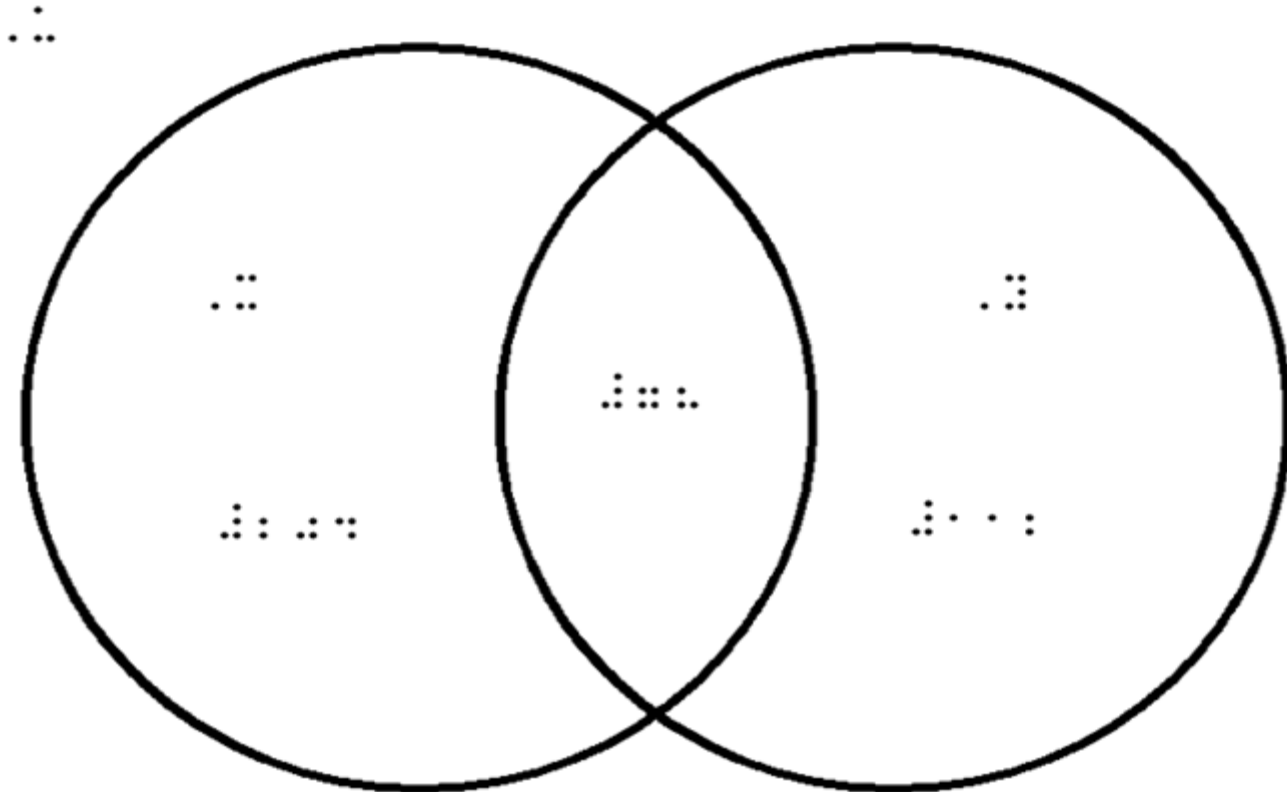


# Student-Generated Graphics on a Coordinate Plane

- APH Graphic Aid for Mathematics
- Graph Paper

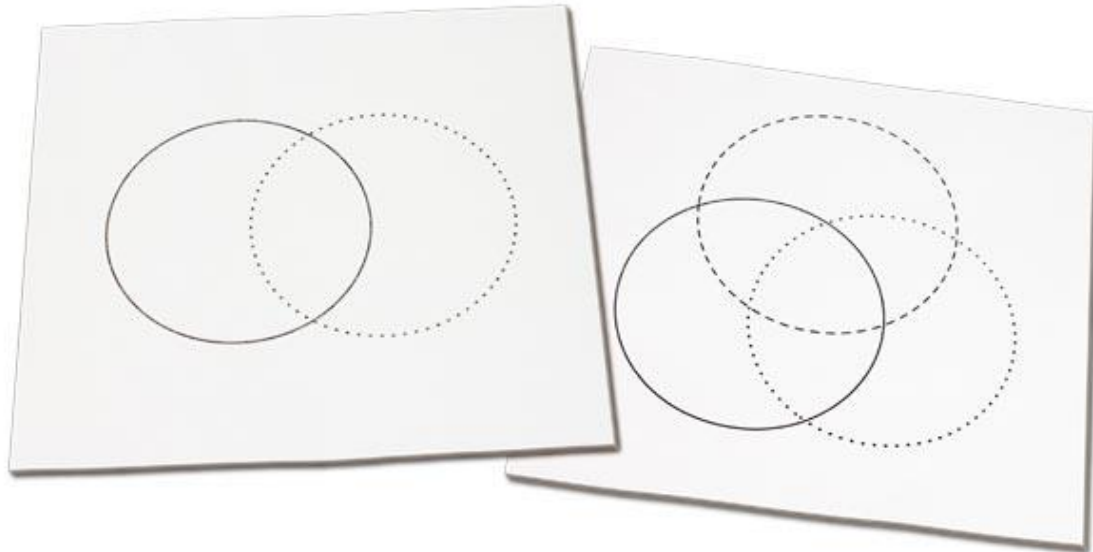


# Student- or Teacher-Generated Venn Diagram



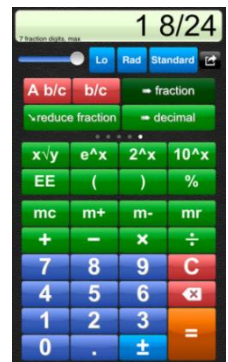
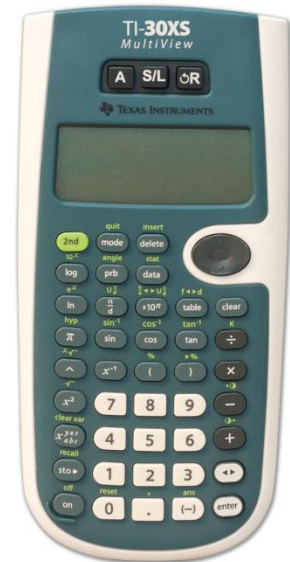
# Venn Diagram Template Kit

[www.aph.org](http://www.aph.org)



# Talking Scientific Calculators

- ORION TI-36X  
[www.orbitresearch.com](http://www.orbitresearch.com)
- ORION TI-30XS  
[www.apf.org](http://www.apf.org) (available on federal quota money)
- SciPlus-2300 Scientific Calculator with speech  
[www.sightenhancement.com](http://www.sightenhancement.com)
- Talking Scientific Calculator  
By Adam Croser  
<https://itunes.apple.com/us/app/talking-scientific-calculator/id411433609?mt=8>



# Notetaker Scientific Calculators

## PAC Mate (BX or QX)

- Talking Scientific Calculator with refreshable braille
- [www.freedomscientific.com/](http://www.freedomscientific.com/)



## BrailleNote Apex (BT or QT)

- Talking Scientific Calculator with refreshable braille
- [www.humanware.com](http://www.humanware.com)



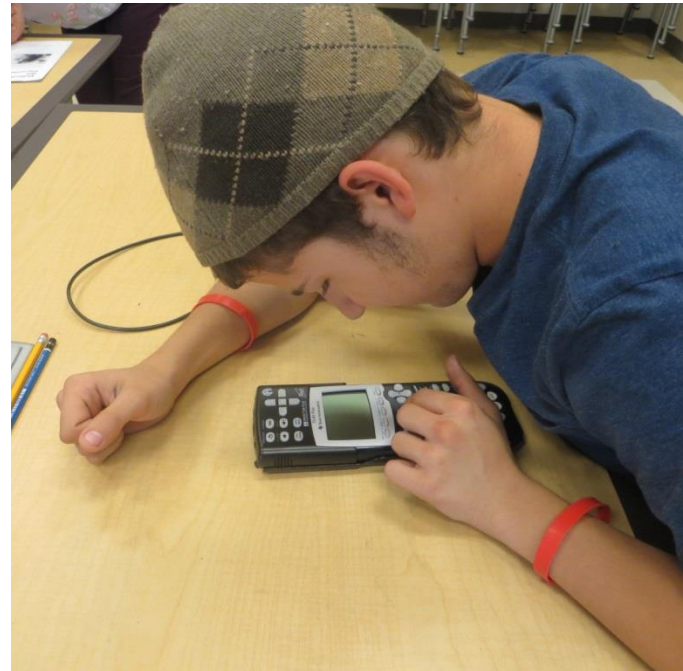
## Braille Sense U2 or QWERTY

- Talking Scientific Calculator with refreshable braille
- <http://hims-inc.com>



# ORION TI-84+ Talking Graphing Calculator

- Now available from APH [www.aph.org/](http://www.aph.org/)



# DESMOS

## [www.desmos.com/accessibility](https://www.desmos.com/accessibility)

Desmos | Accessibility

Secure | <https://www.desmos.com/accessibility>

What is Desmos? Desmos is the next generation of graphing calculator: in-browser, beautiful, and free! [Try it out >](#)

desmos

About Partnerships Classroom Activities We're Hiring!

Why Accessibility is Important

Supported Browsers

Configuring Your Screen Reader

Expression Entry

Typing Symbols

Table Entry

Sliders

Audio Tracing

Slider Trace

Common Actions

Mobile App

We Would Love Your Feedback

Desmos Graphing Calculator

Untitled Graph Save

desmos

Audio trace on

$y = x^2 - \frac{1}{2}$

$y = \cos(x)$

Playing audio 2:11 / 2:53

Why Accessibility is Important

Our mission at Desmos is to help every student learn math and love learning math. Our graphing calculator is used by millions of students all around the world, and we'd like to see that use expand

# DESMOS

<https://www.desmos.com/accessibility>

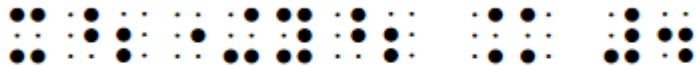
<https://www.desmos.com/braille-demo/index.html>

<https://www.desmos.com/scientific?braille>

Braille

Nemeth

UEB



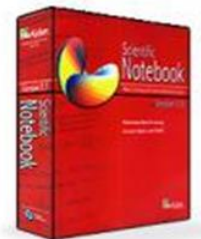
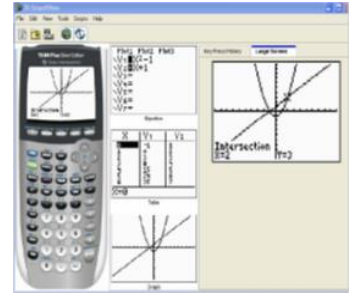
Formatted Math

$$x^2 + y^2 = 4$$

A screenshot of the Desmos Scientific Calculator interface. The interface is in Braille Mode, as indicated by the settings menu in the top right corner. The settings menu shows 'Projector Mode' and 'Braille Mode' with options 'Off', 'Nemeth' (selected), and 'UEB'. There is also a checkbox for 'Reverse Contrast'. The main display area shows the equation  $x^2 + y^2 = 4$  in Braille. Below the display, there is a warning message: 'This calculator does not support this type of equation...'. The bottom of the interface features a navigation bar with buttons for 'main', 'abc', 'func', 'DEG', and 'clear all'. A large grey box at the bottom states 'Braille Mode Is On!' and provides instructions: 'Try hooking up a Refreshable Braille display, or just type with a keyboard.'

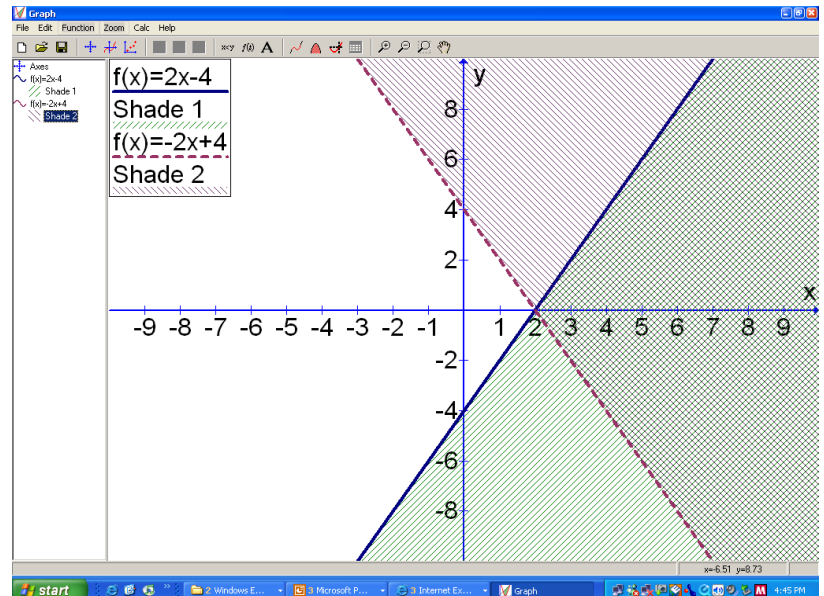
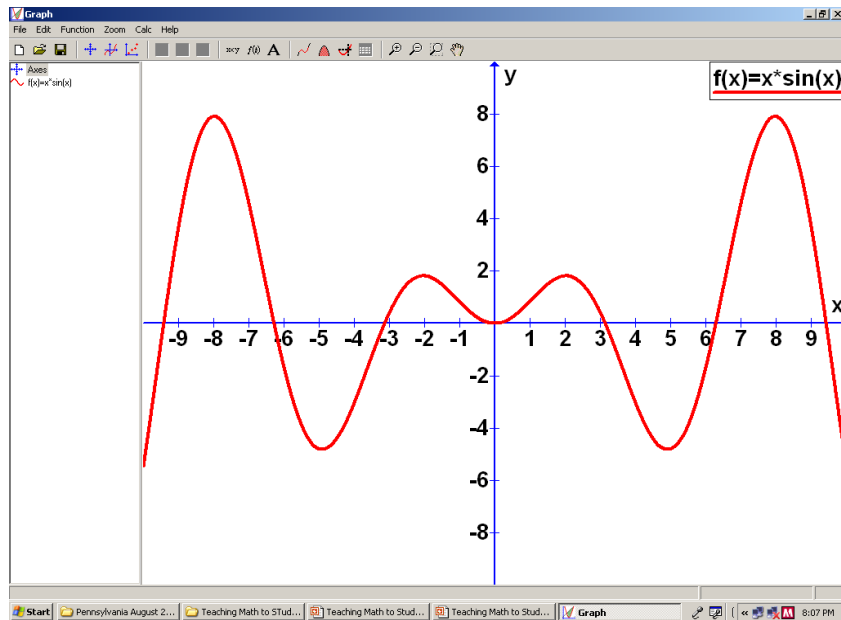
# Large Display Scientific/Graphing Calculator Solutions

- TI-Smart View 2.0  
The Emulator Software  
Package for the TI-84+  
<http://education.ti.com/educationportal/>
- TI-NSpire (or TI-NSpire CAS+)  
<http://education.ti.com/en/us/nspire-family/cx-handhelds/>
- SciPlus-2200 Scientific Calculator  
[www.sightenhancement.com/](http://www.sightenhancement.com/)
- Scientific Notebook  
[www.mackichan.com](http://www.mackichan.com)



# Large Print Graphs by *Graph*

[www.padowan.dk](http://www.padowan.dk)



# Large Display Graphing Calculator Solutions on a Tablet

- Desmos Graphing Calculator (available for iPad and Android)
- Free Graphing Calculator by William Jockusch (available for iPad and Android)



# Publications and Videos (Algebra)

- Osterhaus, S.A. (2002). Susan's Math Technology Corner: Teaching A Blind Student How to Graph on a Coordinate Plane: No Tech, Low Tech, and High Tech Tools. *Division on Visual Impairments Quarterly*, 47(3), 23-26  
[www.tsbvi.edu/index.php?option=com\\_content&view=article&id=3619:coordinate-plane&catid=54](http://www.tsbvi.edu/index.php?option=com_content&view=article&id=3619:coordinate-plane&catid=54)  
[www.tsbvi.edu/videos-webinars/mathematics](http://www.tsbvi.edu/videos-webinars/mathematics)
- Solving Quadratic Equations Graphically, by Factoring, and by Using the Quadratic Formula  
[www.tsbvi.edu/resources-math/3237-teaching-strategies#Quadratic](http://www.tsbvi.edu/resources-math/3237-teaching-strategies#Quadratic)

# Videos

[www.tsbvi.edu/videos-webinars/mathematics](http://www.tsbvi.edu/videos-webinars/mathematics)

- Orion TI-36X Talking Scientific Calculator
- Orion TI-84 Tutorials
  - Graphing Simple Functions and Gathering Information
  - Plotting Points and the Line of Best Fit
  - Working with Matrices
- Using the Orion TI-84 Plus in the Classroom

# Geometry

# Hands-on System for Learning Three-Dimensional Geometry [www.geometro.net](http://www.geometro.net)



# Geometro Sets Now Available from APH

[www.aph.org](http://www.aph.org)

Mini



Medium

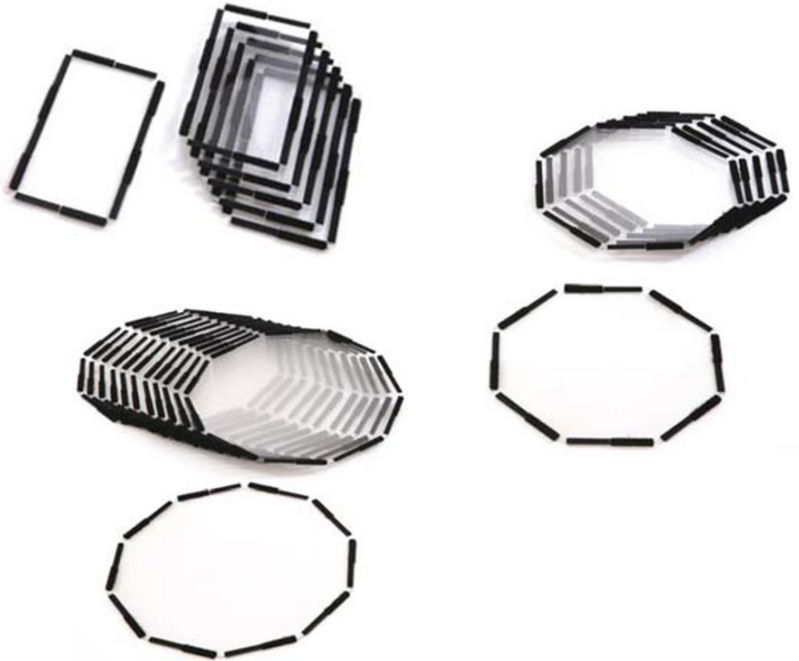
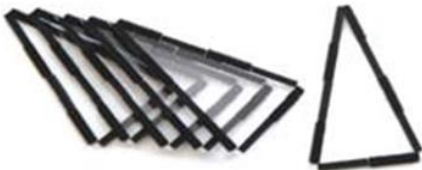


Large



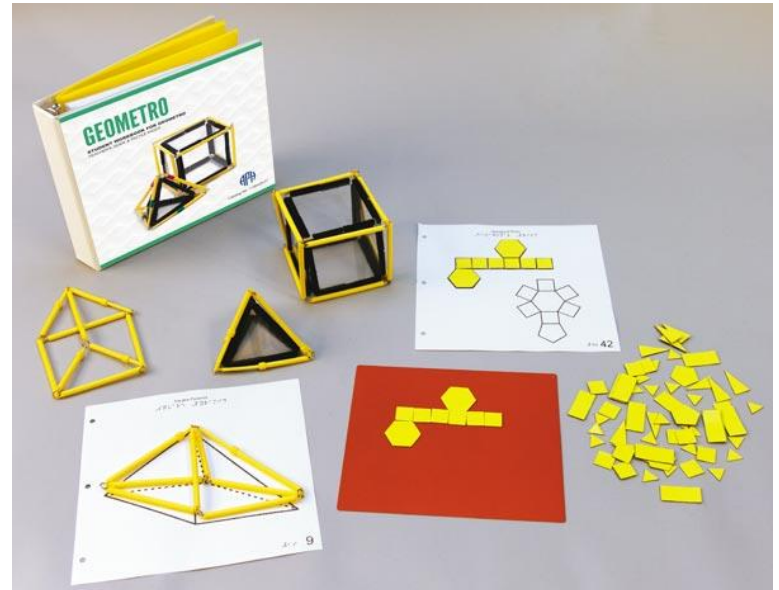
# More Geometro Shapes

- Rectangles
- Octagons
- Decagons
- Isoceles Triangles
- Hook Material Rods



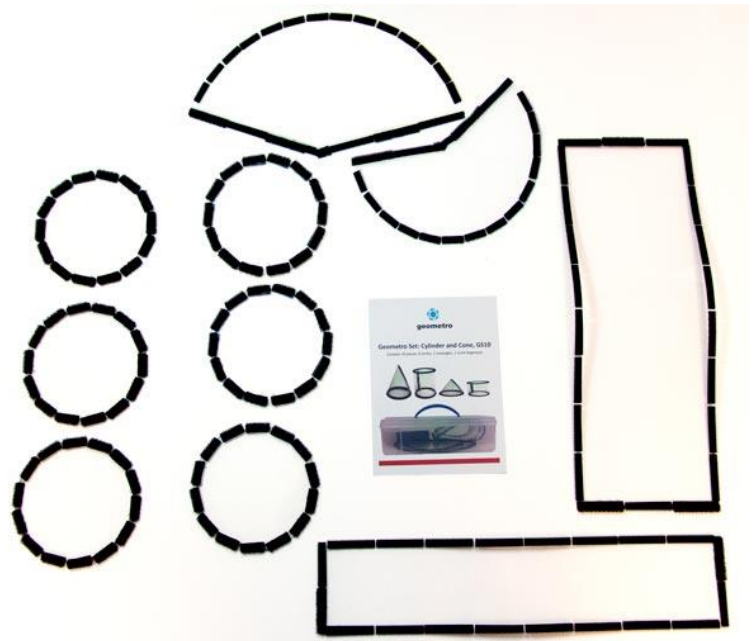
# Geometro: Student Workbook Kit

- Familiarize students with various 3-D solids and their general properties
- Help students grasp the difficult concepts of how 3-D solids relate to their 2-D representations
- Help students understand how 3-D objects are made with 2-D objects



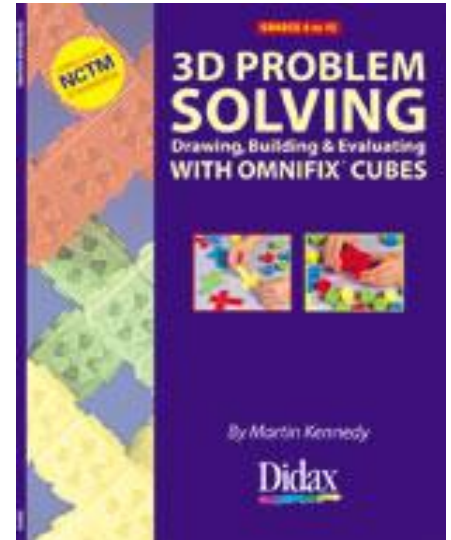
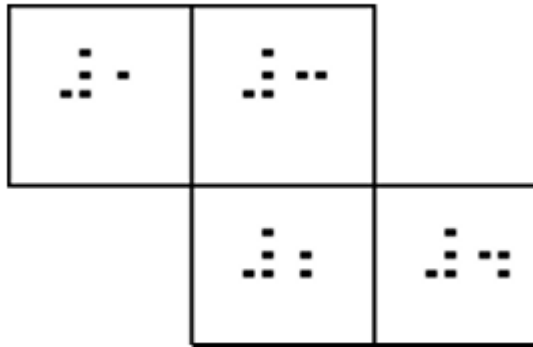
# Geometro GS10 Cylinder and Cone

- Provides students with flat plastic shapes (six circles, two rectangles, and two circle sectors) that can be readily joined to form two cylinders and two cones. Each have the same base, but different heights.



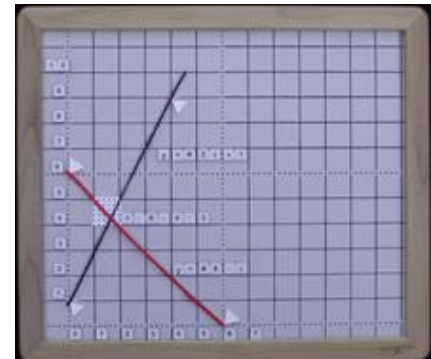
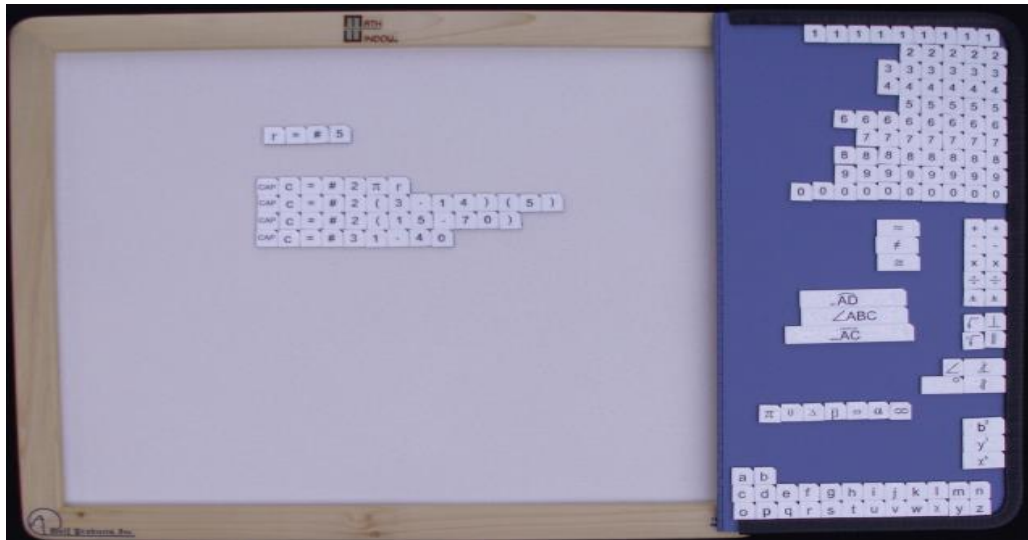
# Omnifix Cubes

[www.didax.com](http://www.didax.com)

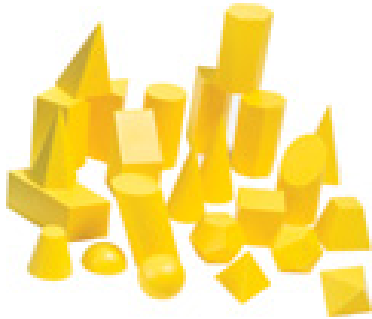


# Math Window Geometry Kit

[www.mathwindow.com](http://www.mathwindow.com)



# Geometric Manipulatives



- Didax Plastic Geometric Models 25 shapes
- Discovery Toys Playful Patterns Design
- Didax 4 Geometric Templates

# Drawing/Construction Tools

- Drawing Board
- Compass

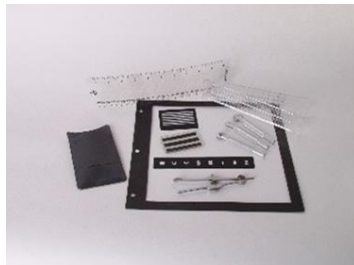
[www.maxiaids.com](http://www.maxiaids.com)

[www.fiskars.com](http://www.fiskars.com)

[www.APH.org](http://www.APH.org)

[www.staedtler.us/en/](http://www.staedtler.us/en/)

[www.easytactilegraphics.com/](http://www.easytactilegraphics.com/)



# Drawing/Construction Tools (cont.)

- Protractor
- Straightedge
- Tracing Wheel
- Stylus and/or Pen
- Drawing Board

[www.APH.org/](http://www.APH.org/)



# Publications and Videos (Geometry)

- Geometric Constructions  
[www.tsbvi.edu/resources-math/3237-teaching-strategies#Geometric](http://www.tsbvi.edu/resources-math/3237-teaching-strategies#Geometric)  
[www.tsbvi.edu/videos-webinars/mathematics](http://www.tsbvi.edu/videos-webinars/mathematics)
- Transformations, Line Symmetry, and Tessellations  
[www.tsbvi.edu/resources-math/3237-teaching-strategies#Transformations](http://www.tsbvi.edu/resources-math/3237-teaching-strategies#Transformations)
- APH Braille/Print Protractor  
[www.tsbvi.edu/videos-webinars/mathematics](http://www.tsbvi.edu/videos-webinars/mathematics)

# Other Math Resources

- Delta [www.delta-education.com](http://www.delta-education.com)
- Didax [www.didax.com](http://www.didax.com)
- ETA Hand2Mind [www.hand2mind.com](http://www.hand2mind.com)
- Math Forum [www.mathforum.org](http://www.mathforum.org)
- Nasco [www.enasco.com/math](http://www.enasco.com/math)
- Online Math Tutorial Videos  
[www.tsbvi.edu/videos-webinars/mathematics](http://www.tsbvi.edu/videos-webinars/mathematics)

Thank you for your kind attention.

Now, it's time for questions...