

# Tools and Best Practices for Helping Blind Elementary School Students Succeed in Mathematics

**Sponsored by:**

National Organization of Parents of Blind Children  
Division (NOPBC)

NFB Convention  
ORLANDO, FLORIDA  
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Presented by  
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Impaired

Outreach Programs

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[www.tsbvi.edu/math](http://www.tsbvi.edu/math)

[www.tsbvi.edu/videos-webinars/mathematics](http://www.tsbvi.edu/videos-webinars/mathematics)

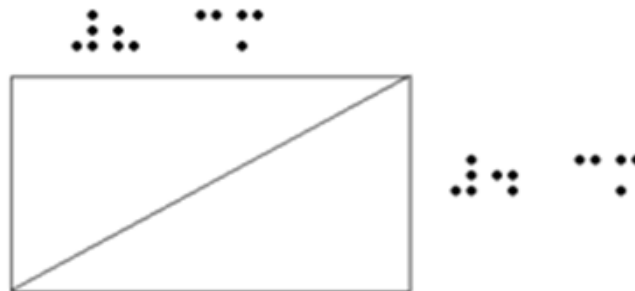
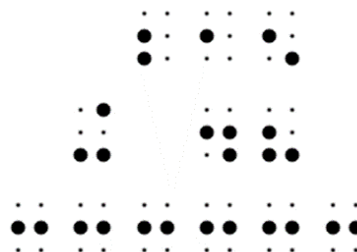
# Agenda

- Math Materials (Including Graphics)
  - Braille Reader
  - Low Vision Student
- Accessible Math Tools and Technology
  - Number and Quantity
  - Measurement
  - Algebra and Statistics and Probability
  - Geometry

# Math Materials

## Braille Reader

- High Quality Braille Textbooks & Assessments (Including Released Tests)
  - Nemeth Code
  - Tactile Graphics
- Teacher-Made Materials
  - Worksheets
  - Quizzes
  - Tests



# What's New with Learning Nemeth!

- *Guidance for Transcription Using the Nemeth Code within UEB Contexts*, Approved June 2016 (Revised 2018)  
[www.brailleauthority.org/mathscience/math-science.html](http://www.brailleauthority.org/mathscience/math-science.html)
- *Nemeth at a Glance: A Math Resource, Grade Level Chart, and Evaluation Tool*  
<http://www.tsbvi.edu/store/ecom/index.php?action=ecom.pdetails&mode=nemeth>
- Nemeth Braille Code Curriculum:  
<http://accessibility.pearson.com/nemeth/>

# Accessible Equation Editor

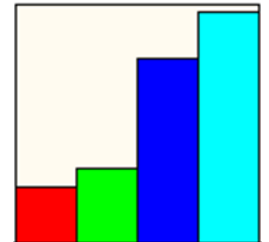
<http://accessibility.pearson.com/mathex-app/>

The image shows the interface of the Accessible Equation Editor. At the top is a horizontal toolbar with icons for basic arithmetic (+, -, ×, ÷), fractions, exponents ( $y^x$ ), square roots ( $\sqrt{\quad}$ ), equals (=), approximate ( $\approx$ ), undo, redo, delete, a grid of dots, and a clear button. Below the toolbar is a large text input area containing the equation  $\sqrt{25} = \pm 5$ . To the right of the input area is a sidebar with a scrollable list of categories: Arithmetic, Fractions, Exponents, Functions, Groups, Relations, Omissions, and Sets. The 'Arithmetic' category is expanded, showing a sub-toolbar with buttons for +, -, ×, ÷, a decimal point, a fraction bar, ±, ∓, \*, [ / ], +-, -+, x!, and ÷. At the bottom of the interface is a Braille display showing the Braille representation of the equation  $\sqrt{25} = \pm 5$ .

# Math Materials

## Large Print Reader

- Large Print Textbook
- Enlarged Materials
- Regular Print with Magnification
- Be Alert for Color-Keyed Graphics



# Accessible Math Graphics

- Tactile Graphics
- Large Print Graphics
- Universally Designed Math Graphics for both the Student Who is Blind or Who Has Low Vision



# *Guidelines and Standards for Tactile Graphics, 2010*

from the Braille Authority of North America  
(BANA) and Canadian Braille Authority (CBA)

[www.brailleauthority.org/](http://www.brailleauthority.org/)

Available for purchase from APH...

Print: 7-35935-00      Braille: 5-35935-00

# *Guidelines and Standards for Tactile Graphics*

## *Supplement: Examples 1 - 35*

The tactile graphics examples illustrated in this supplement have been designed to accompany the *Guidelines and Standards for Tactile Graphics 2010*. Each tactile graphic is preceded by a brief summary of the important design techniques and braille formats used in each example.

Available for purchase from APH...

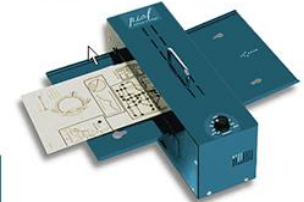
Print: 7-35936-00      Braille: 5-35936-00

# Tactile Imaging Machine and Swell Touch Paper

- Pictures in a Flash (PIAF)  
[www.humanware.com](http://www.humanware.com)

PIAF - Pictures In A Flash

Tactile graphics made 1-2-3 easy!



A Simple and Fast Way to Produce Tactile Graphics

- Swell-Form Graphics Machine  
[www.americanthermoform.com](http://www.americanthermoform.com)



# ViewPlus Braille Embossers are all Powered by Tiger®



[www.viewplus.com](http://www.viewplus.com)



- **Braille production made flexible and easy:**  
Braille is translated and embossed from MS Word in one touch and graphics are produced from any PC software including Illustrator & CorelDraw.
- **Braille and Ink:**  
Prints Braille and ink on the same page in a single pass.
- **Tactile graphics embossed in fine detail:**  
Tiger tactile graphics are the highest-resolution of any embosser.
- **Braille & graphics software included:**  
TSS incorporates braille software, tactile graphic studio, and more. It is also compatible with Duxbury and other braille software.

# Phoenix Braille and Tactile Graphics Embosser

<http://brailleur.com/phoenix.php>



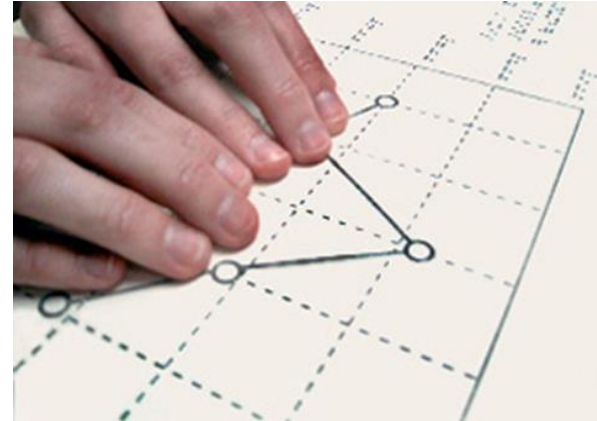
- Introducing Phoenix, the World's first multi-function Braille and Tactile Graphics System.
- Imagine the ability to scan your pictures, graphs and charts into your computer and with a few clicks of the mouse, emboss those images in high definition tactile graphics without compromising the quality of your Braille text.

# Math Graphics Made to Order by Others

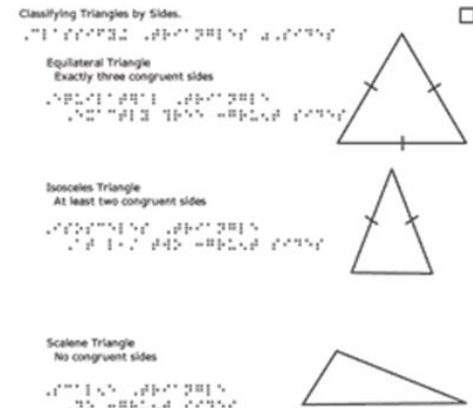
- gh, LLC

LaserLine™ Graphics

[www.gh-accessibility.com](http://www.gh-accessibility.com)

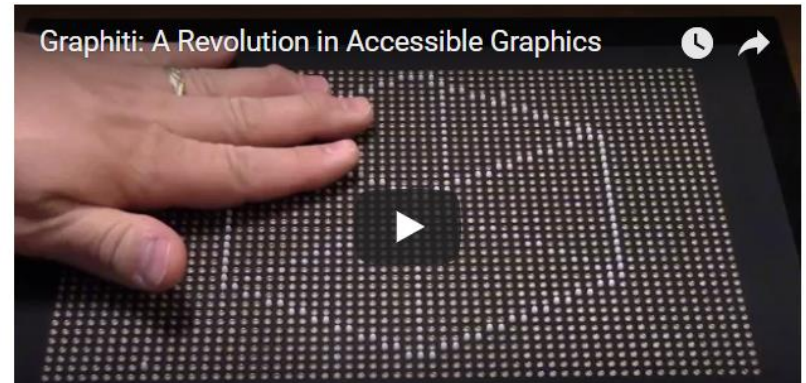


- Tactile Vision Graphics  
<http://tactilevisiongraphics.com>



# Graphiti [www.aph.org](http://www.aph.org)

- **Graphiti is a dynamic multilevel tactile touch display** developed by [Orbit Research](http://OrbitResearch.com) and the American Printing House for the Blind. Graphiti allows students and adults to access a wide variety of on-screen graphics by touch.



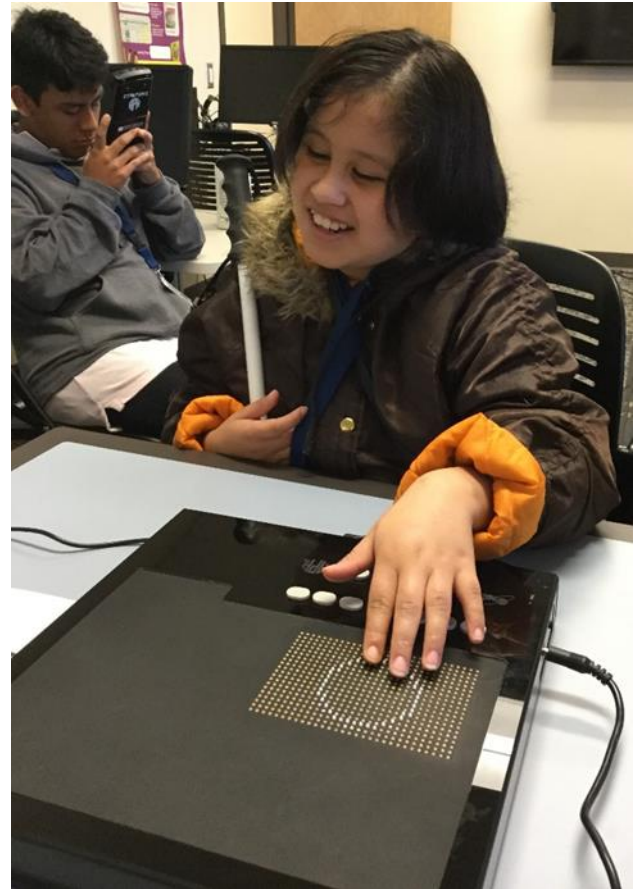


# Graphiti – Short Term Programs' Math Tools Class - Guess the Shape

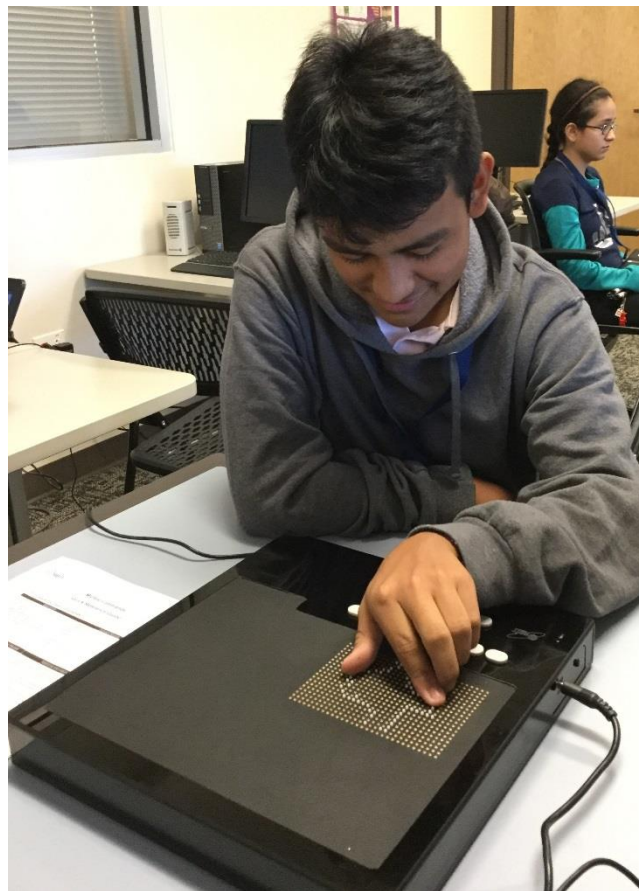
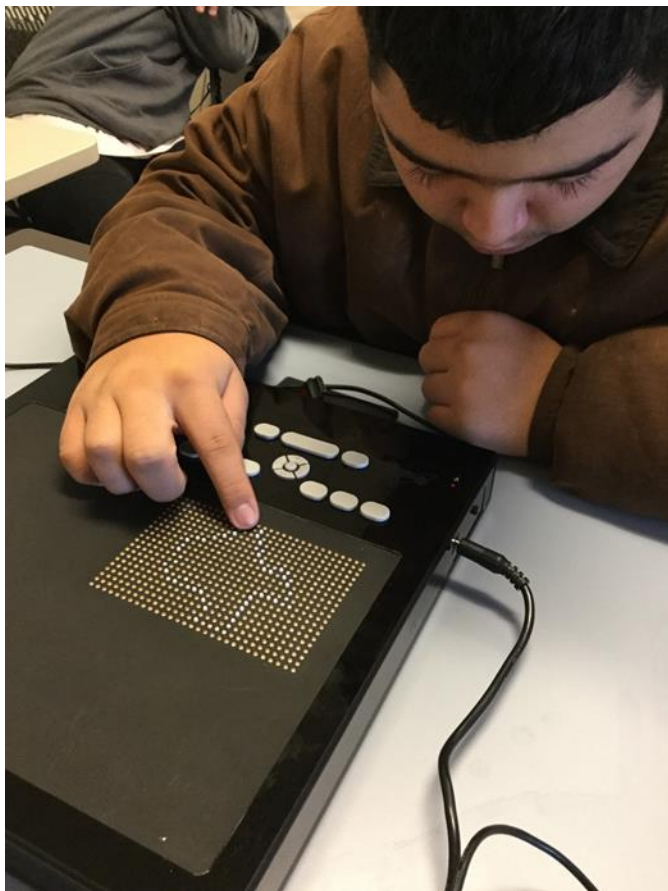




# Graphiti – Triangle and Circle



# Graphiti – Is that Texas?



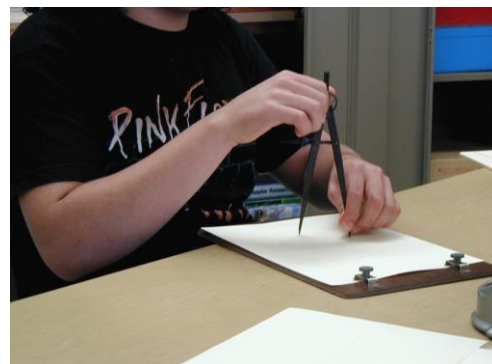
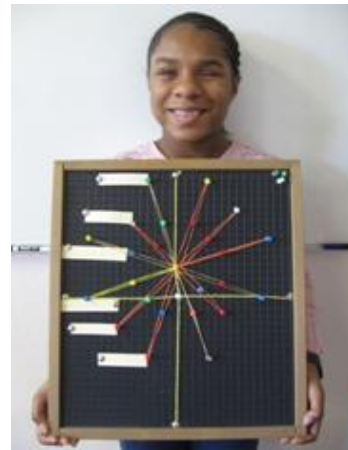
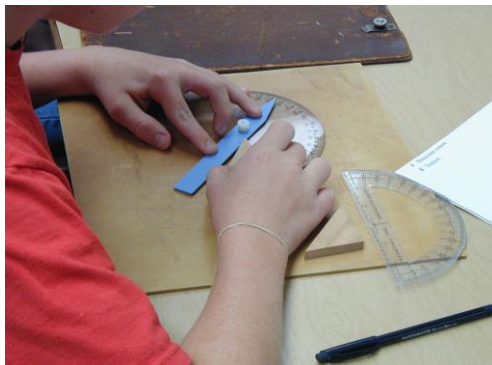
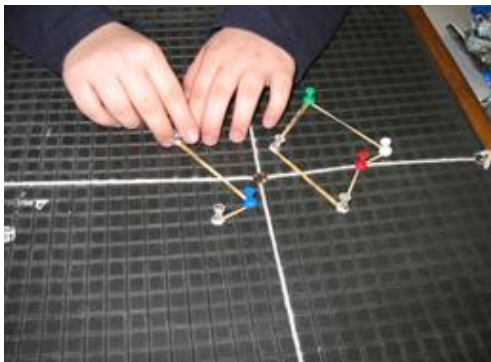
# Thoughts on Visual vs Tactual Perception

1. Visual impairment is not an isolated condition; it affects the whole process of information-gathering.
2. Vision enables a person to simultaneously perceive all parts of an object in its totality and in its relationship to other objects.
3. The learner who is visually impaired has to rely on sequential observations (only part of an object can be seen or felt at a time), and the entire image has to be "built-up" out of the components. Relationships with other objects can be lost entirely.
4. The level of cognition needed for integration of sequential information is higher than that needed for concept formation through immediate visual perception.
5. If you have vision, you can experience this way of processing information by looking at a drawing through a very small hole in a piece of card held over the drawing; I think that you will find that it's hard for you to "get the picture."

# Teaching Students How to Read Tactile Math Graphs

- Begin at an early age
- Start with real objects
- Move to 3-D models
- Then to 2-D manipulatives
- Finally try tactile graphics on various surfaces
  - Hard plastic
  - Thermoformed Brailon of foil or collage
  - Capsule/Swell/Flexi-Paper
  - Braille Paper
- Use the APH Tangible Graphs Kit to evaluate and/or re-teach if necessary.

# Accessible Math Tools and Technology





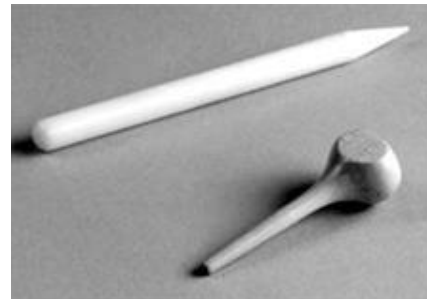
# Basic Math Tools

## Braille Reader

- Braillewriter
- Braille Paper



- Braille Eraser



# Basic Math Tools

## Large Print Reader

- Appropriate Paper
  - Bold line paper
  - Unlined paper
- Proper Writing Implement
  - Sharpie
  - 20/20
  - Flair
  - Staedtler Mars Technico Mechanical Pencil

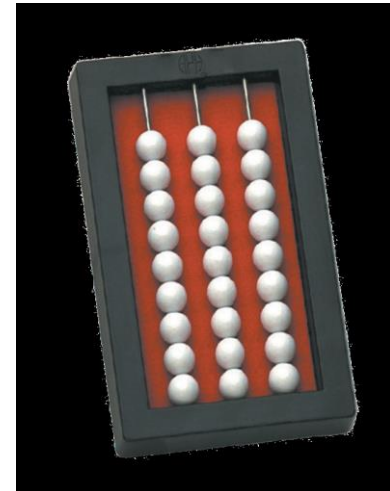
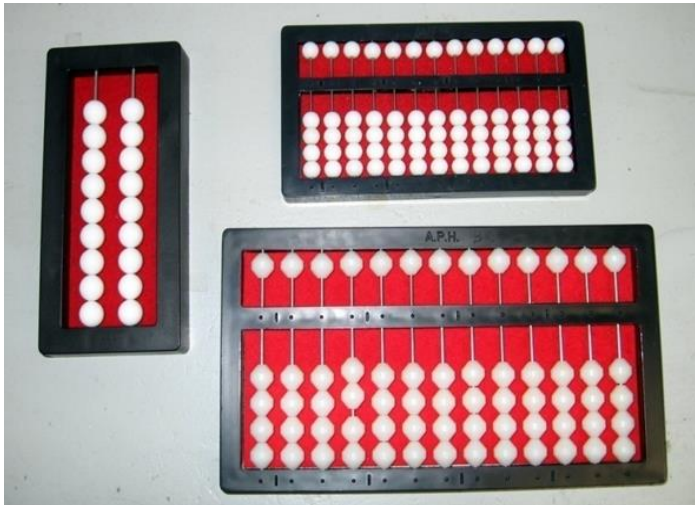


# Number and Quantity

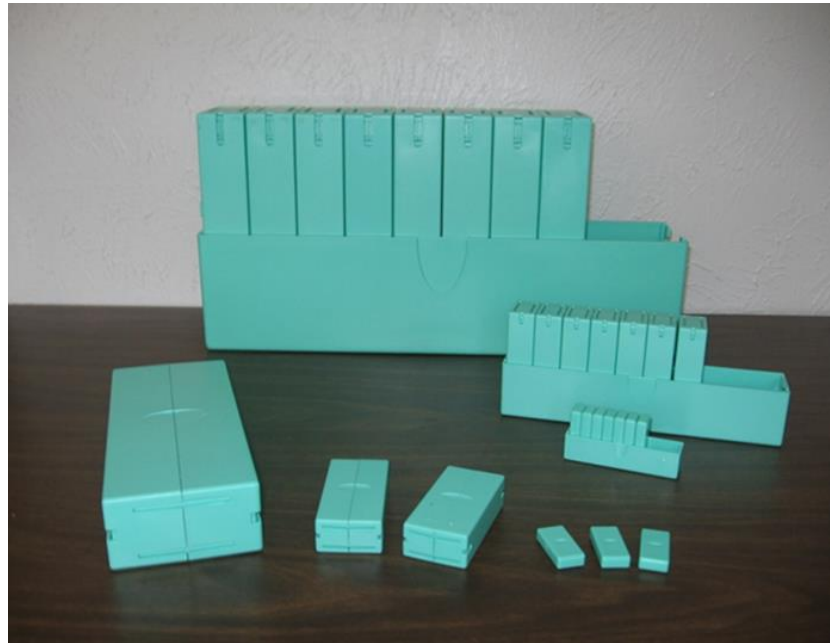


# Abaci from APH [www.aph.org](http://www.aph.org)

- Cranmer Abacus
- Beginner's Abacus Kit
- Expanded Beginner's Abacus Kit



# Manipulatives to Enhance Number System Concepts

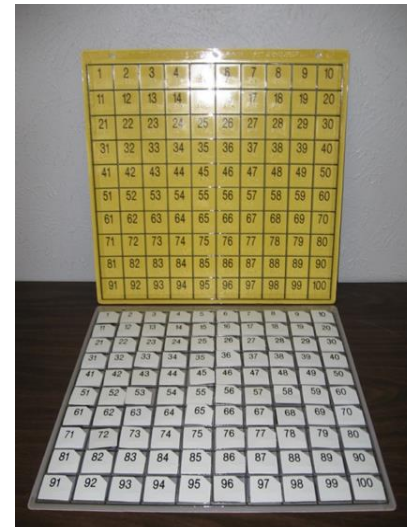
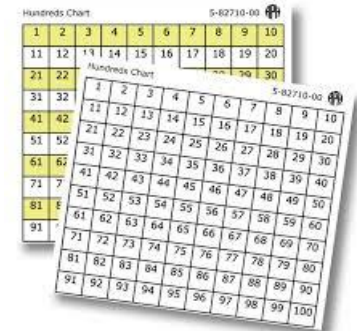


Digi-Blocks [www.digiblock.com/](http://www.digiblock.com/)

# APH Tools to Enhance Number System Concepts

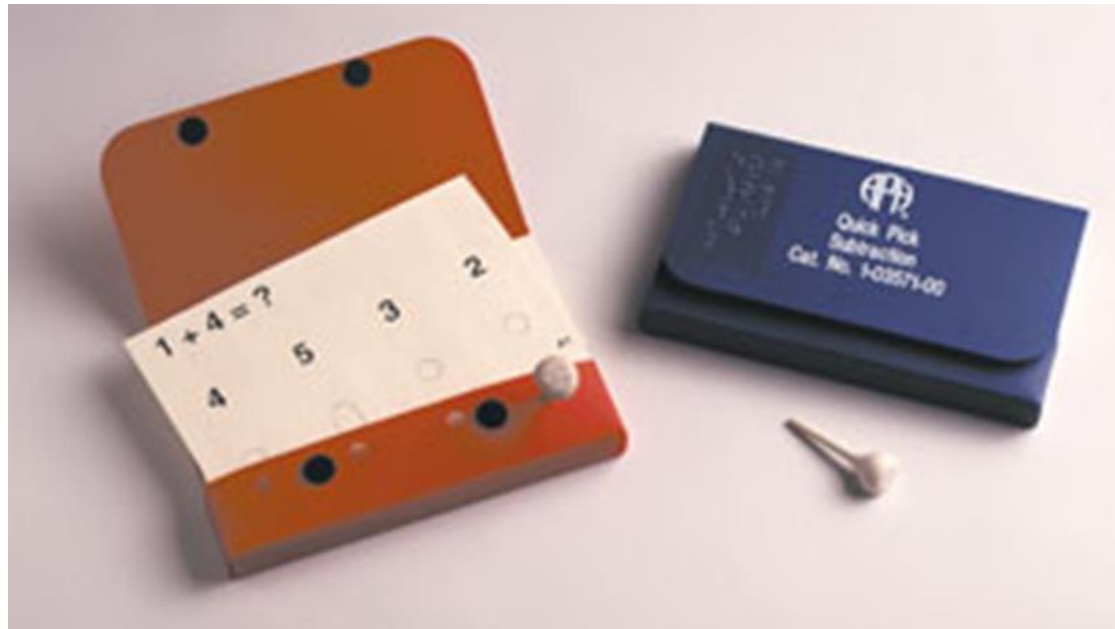
- Braille & LP  
“Numbers to 100” Charts

[www.aph.org](http://www.aph.org)



# APH Tool to Help Increase Basic Math Skills

- Quick Pick: Math



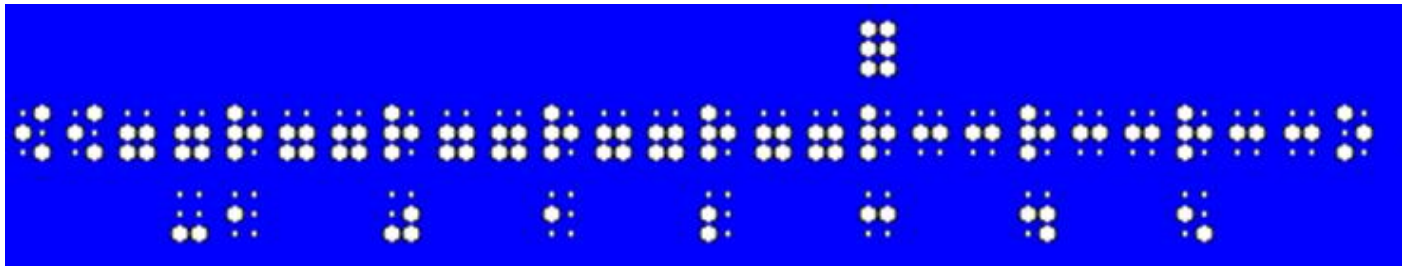
# Fractions

- Fraction Pies
- Fraction Tiles
- Fractions for Dessert



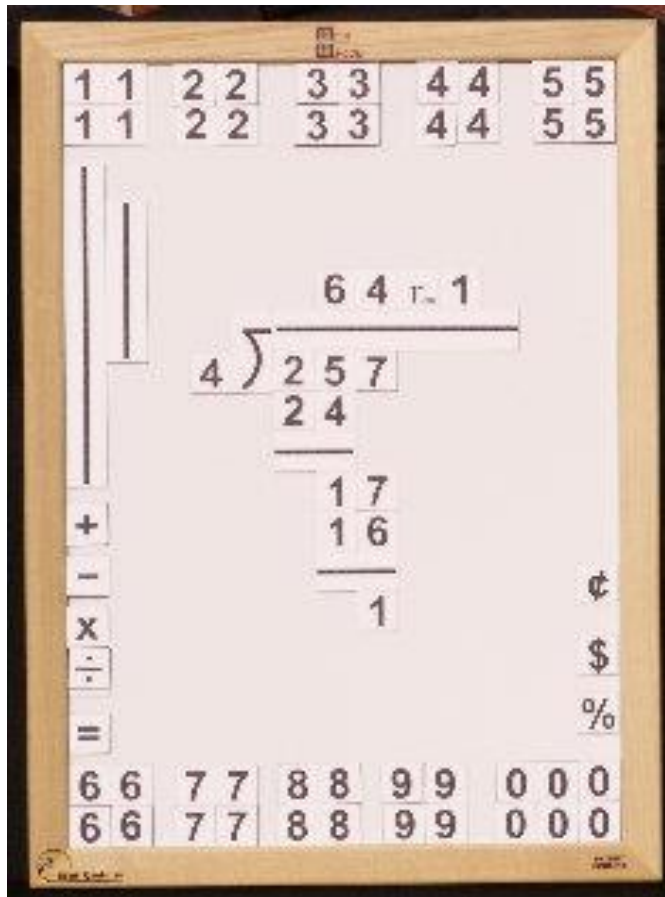
# Student-Generated Graphics on a Number Line

- APH Number Line Device
- APH Consumable Number Lines
- Desktop Stick-On Number Lines
- Student-Made Number Lines





# Hands-On Computation Tool



Math Window in Braille  
and Large Print

[www.mathwindow.com](http://www.mathwindow.com)

# APH Math Apps

<http://www.aph.org/products/mobile-apps/>



- Math Flash (Action for Google Home/Google Assistant) Based on APH's popular Math Flash™ software that combines math flash cards with fun audio feedback and animated characters!



- Slapstack Math (for iOS devices) Slapstack Math™ is an action and memory game that uses math flash cards instead of playing cards. The goal is to collect the most points by pulling in the most cards.



# Math Robot™ from APH

<https://itunes.apple.com/app/math-robot/id704570512>

- Math Robot iOS App
  - Works with your iPad or iPad mini running iOS 7 or later!
  - Use with a refreshable braille display





- <http://awvis.arizona.edu>
- [www.aph.org](http://www.aph.org)

# Publications and Videos

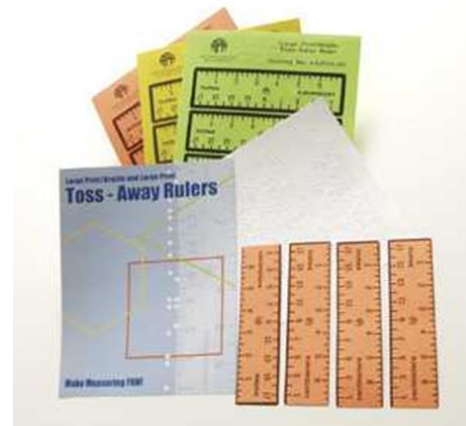
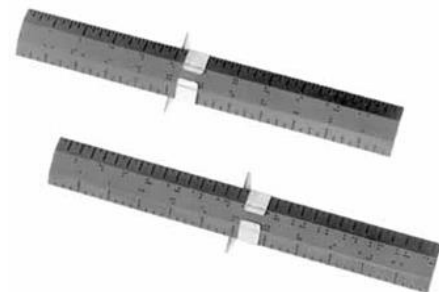
- Abacus: Getting Started with the Counting Method
- Prime Factorization on the Abacus  
[www.tsbvi.edu/videos-webinars/mathematics](http://www.tsbvi.edu/videos-webinars/mathematics)
- Osterhaus, S.A. (2003). *Susan's Math Technology Corner: Standardized Braille Number Lines*. *Division on Visual Impairments Quarterly*, 48(2), 9-11  
[www.tsbvi.edu/resources/2316-susans-math-technology-corner-standardized-braille-number-lines](http://www.tsbvi.edu/resources/2316-susans-math-technology-corner-standardized-braille-number-lines)

# Measurement

# Linear and Angle Measurement

[www.tsbvi.edu/tools/2181-math-tools#equipment](http://www.tsbvi.edu/tools/2181-math-tools#equipment)

- Ruler
- Yardstick and Meter Stick
- Toss-Away Rulers
- Protractor

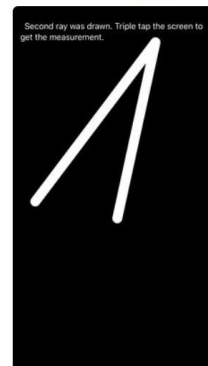


# Draw2Measure Protractor App

<http://www.aph.org/products/mobile-apps/>

- Draw2Measure Protractor App for iOS® devices allows blind and visually impaired students to measure angles in two ways!

First, students can place an angle over the screen of a device, such as a phone or tablet, and trace along the sides of the angle with a fingertip or stylus. The app records the locations of the sides and then calculates the angle.



# Tactile Caliper – 1/16 inch precision

[www.squirreldevices.com](http://www.squirreldevices.com)

[www.youtube.com/watch?v=JOi8zTI9TwY](http://www.youtube.com/watch?v=JOi8zTI9TwY)

- The caliper is accurate to 1/16". There are subtle audible cues when it is operating. The caliper is 12 inches long, the size of a standard ruler. The caliper's design allows for small objects to be inserted into the caliper's opening. This eliminates some common problems for students including holding the ruler steady and lining up the ruler to begin measuring.



The caliper is available from the online store at National Braille Press.

[www.nbp.org/ic/nbp/CALIPER.html](http://www.nbp.org/ic/nbp/CALIPER.html)



# Tactile Caliper – 1 mm Precision

- This metric caliper is brand new and currently being field tested by APH.
- Should be available soon, along with the English measurement tactile caliper, from APH on federal quota funds.





# Temperature



Tactile Demonstration  
Thermometer

[www.aph.org](http://www.aph.org)

# Students at Work Measuring



# Measurement Resources

- Linear Measure, Perimeter, Area  
[www.tsbvi.edu/resources-math/3237-teaching-strategies#Linear](http://www.tsbvi.edu/resources-math/3237-teaching-strategies#Linear)
- APH Braille/Print Protractor  
[www.tsbvi.edu/videos-webinars/mathematics](http://www.tsbvi.edu/videos-webinars/mathematics)

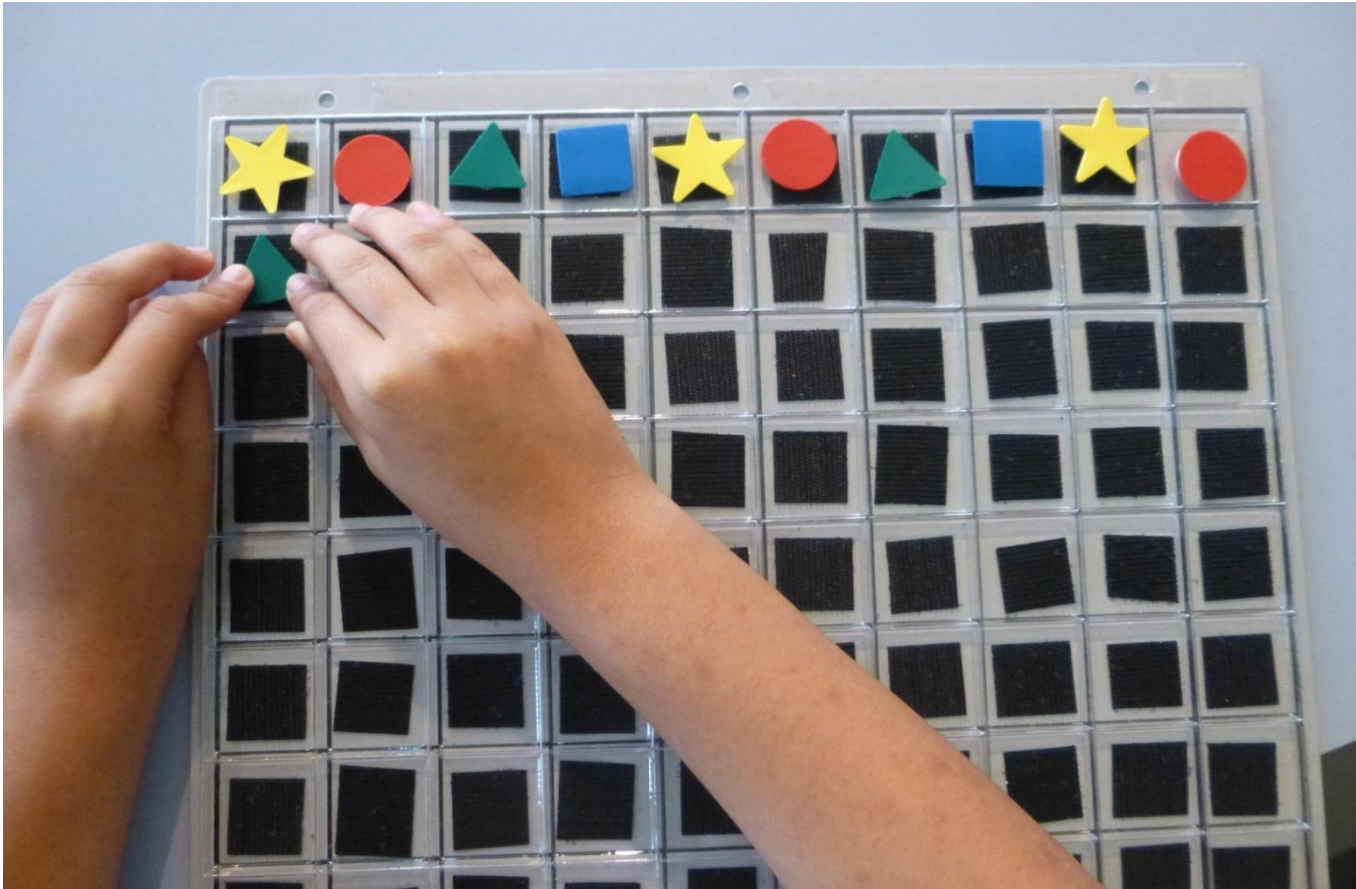
# Algebra and Statistics and Probability

# MathBuilders K-3, Unit 1: Matching, Sorting, and Patterning

[www.aph.org](http://www.aph.org)



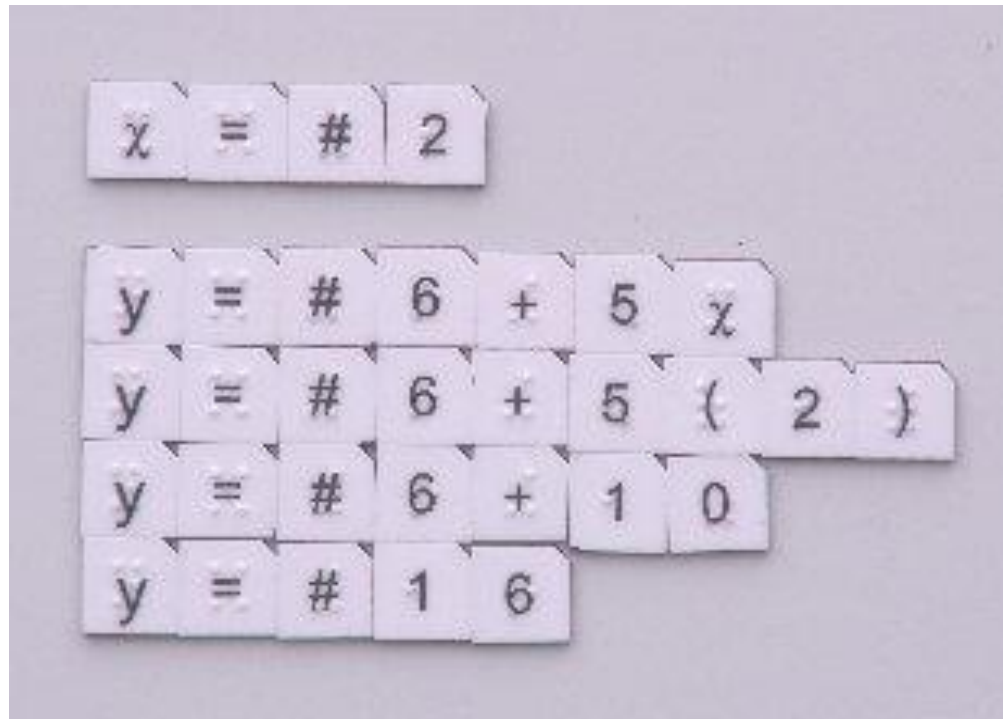
# Patterns on the Hundreds Board





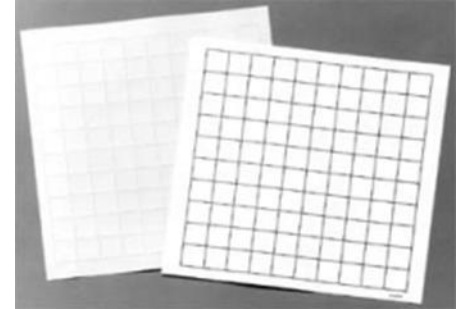
# Math Window Algebra Add-On

[www.mathwindow.com](http://www.mathwindow.com)



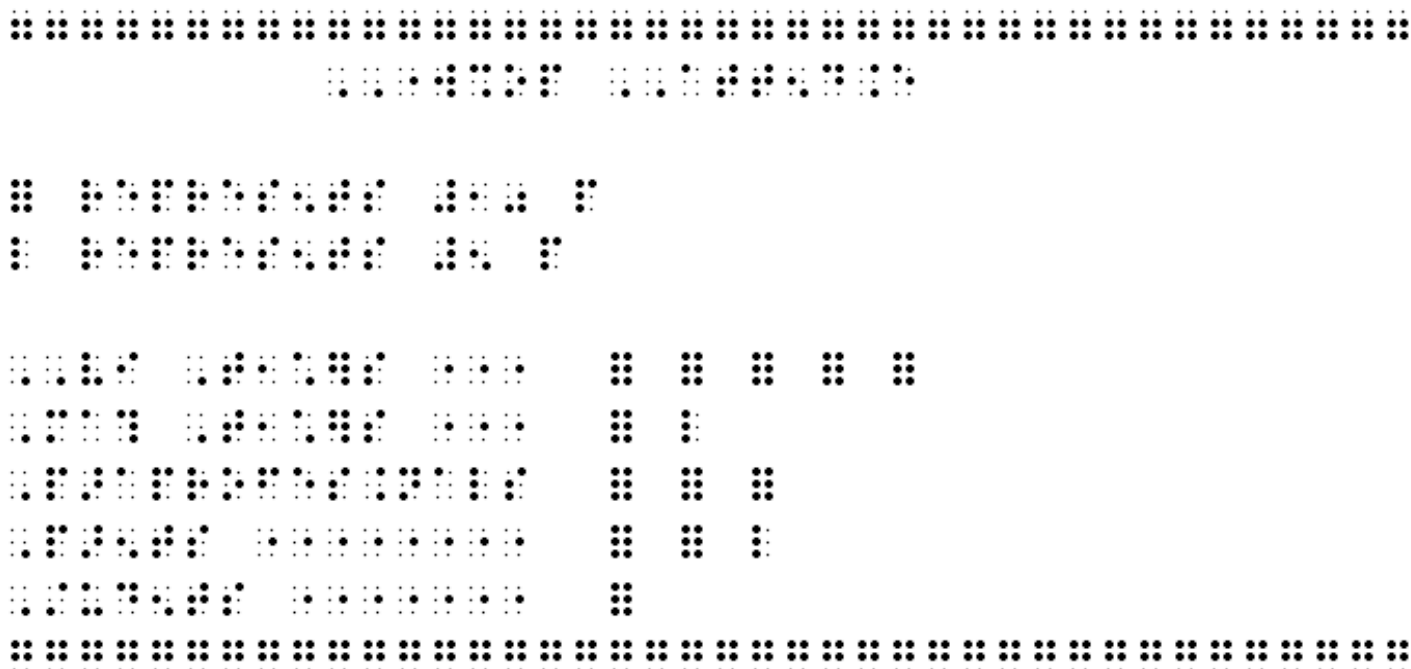
# Student-Generated Graphics on a Coordinate Plane

- **APH Graphic Aid for Mathematics**
- **Graph Paper**

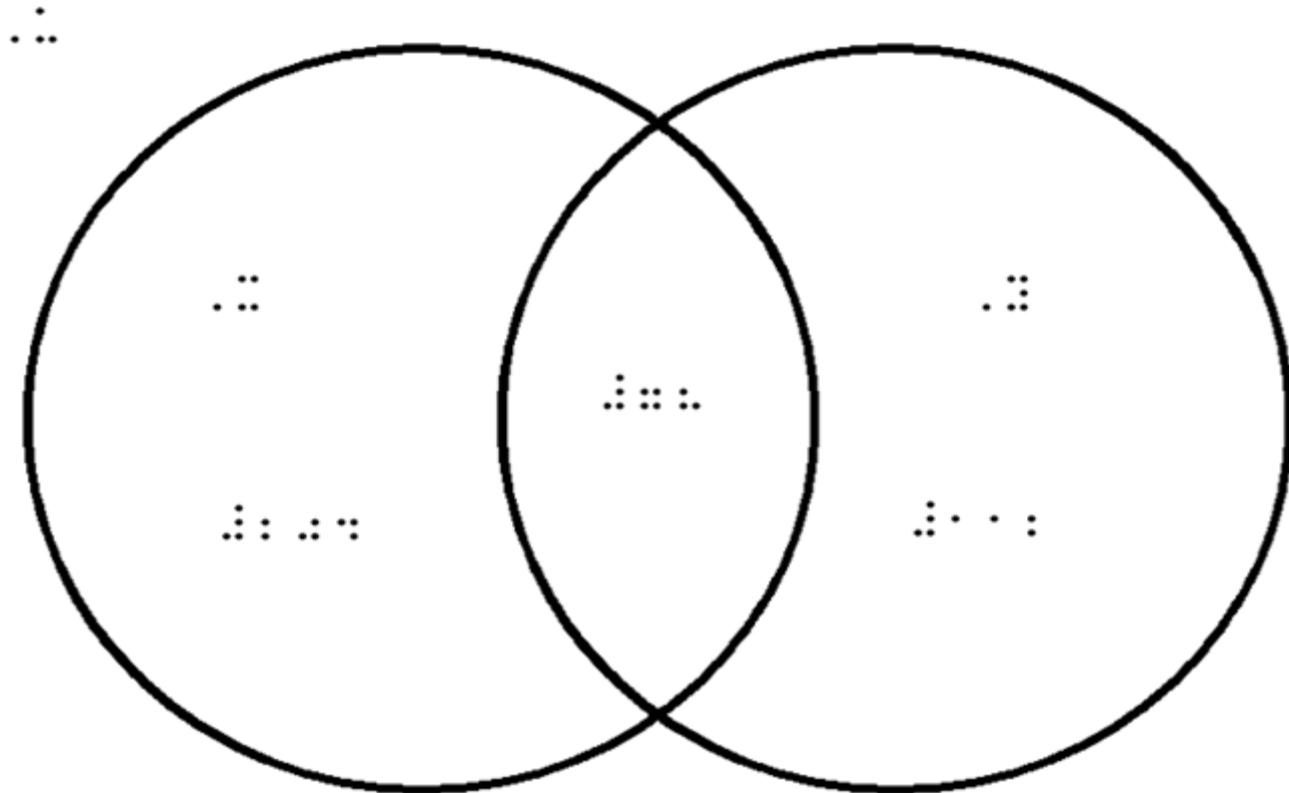




# Student- or Teacher-Generated Braillewriter Pictograph

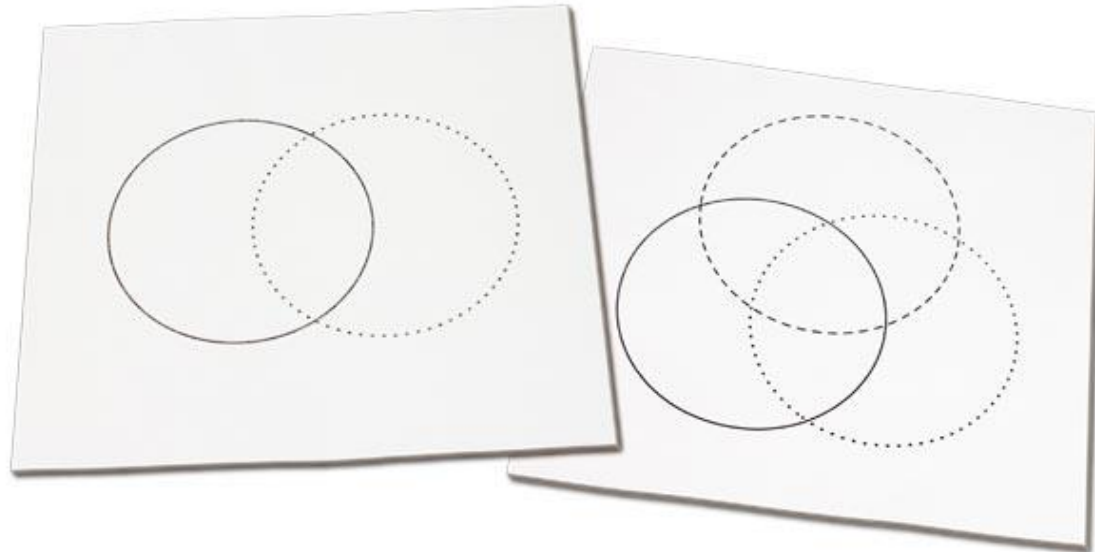


# Student- or Teacher-Generated Venn Diagram



# Venn Diagram Template Kit

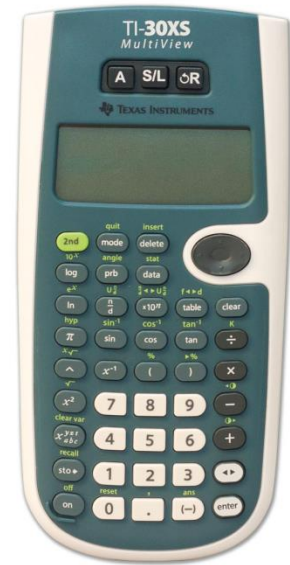
[www.aph.org](http://www.aph.org)



# Talking Scientific Calculators

- ORION TI-30XS

[www.aph.org](http://www.aph.org) (available on federal quota money)



- Talking Scientific Calculator

By Adam Croser

<https://itunes.apple.com/us/app/talking-scientific-calculator/id411433609?mt=8>


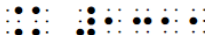


# DESMOS


<https://www.desmos.com/accessibility>

<https://www.desmos.com/scientific?braille>

Your answers show up on this side.




23 · 57 = 1311

main abc func  DEG ↶ ↷ clear all 

**Nemeth is on!**

Use a Refreshable Braille display, or just type Braille with a keyboard.

[Turn Nemeth off](#)

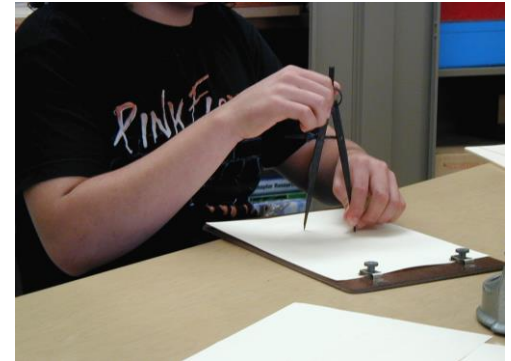
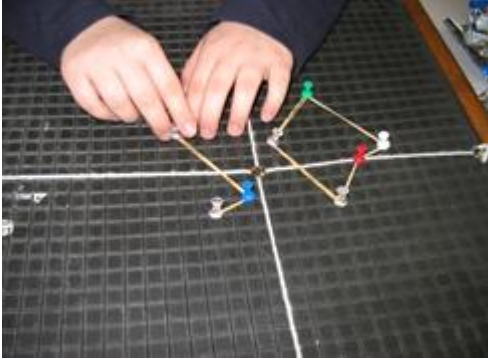
Type this	Nemeth	Typeset
# 2 + 2		2 + 2
? 1 / 2 #		$\frac{1}{2}$
> 4 }		$\sqrt{4}$

[View more examples](#)

# Publications and Videos (Algebra)

- Osterhaus, S.A. (2002). Susan's Math Technology Corner: Teaching A Blind Student How to Graph on a Coordinate Plane: No Tech, Low Tech, and High Tech Tools. *Division on Visual Impairments Quarterly*, 47(3), 23-26  
[www.tsbvi.edu/index.php?option=com\\_content&view=article&id=3619:coordinate-plane&catid=54](http://www.tsbvi.edu/index.php?option=com_content&view=article&id=3619:coordinate-plane&catid=54)  
[www.tsbvi.edu/videos-webinars/mathematics](http://www.tsbvi.edu/videos-webinars/mathematics)

# Geometry



# MathBuilders, Unit 6: Geometry

K-3 [www.aph.org](http://www.aph.org)





# Hands-on System for Learning Three-Dimensional Geometry [www.geometro.net](http://www.geometro.net)



# Geometro Sets Available from APH

[www.aph.org](http://www.aph.org)

Mini



Medium

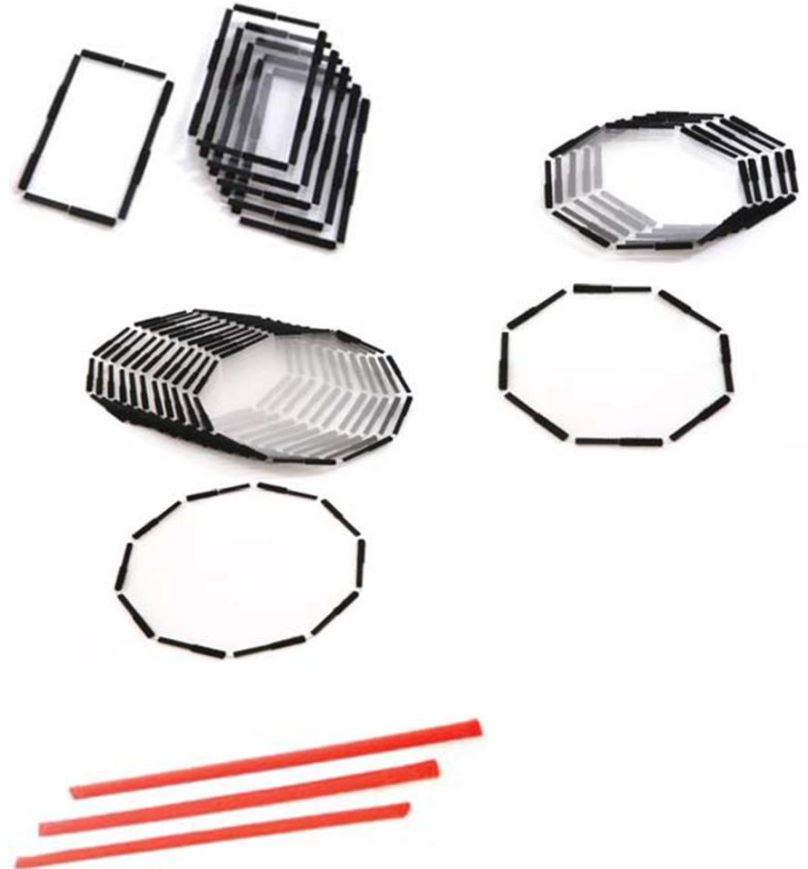
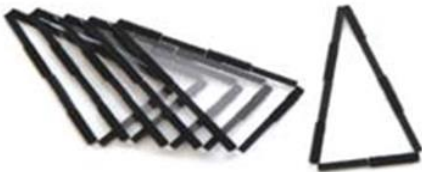


Large



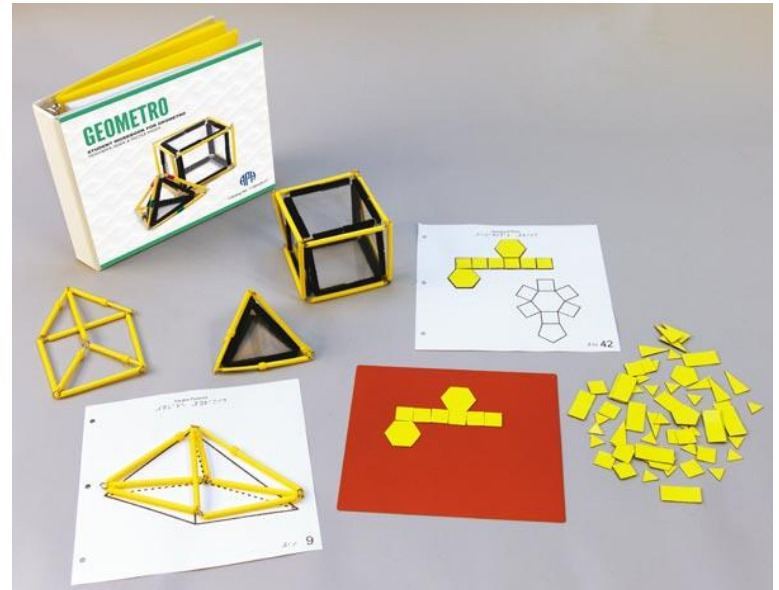
# More Geometro Shapes

- Rectangles
- Octagons
- Decagons
- Isoceles Triangles
- Hook Material Rods



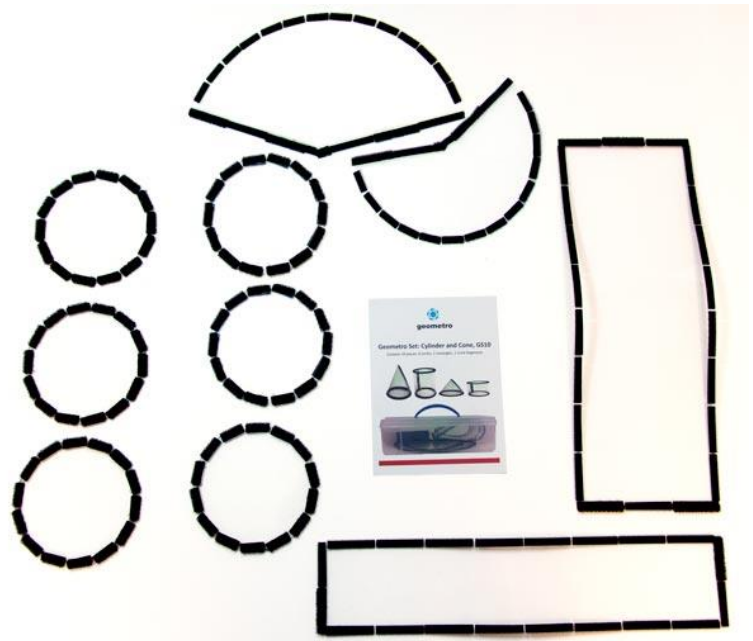
# Geometro: Student Workbook Kit

- Familiarize students with various 3-D solids and their general properties
- Help students grasp the difficult concepts of how 3-D solids relate to their 2-D representations
- Help students understand how 3-D objects are made with 2-D objects



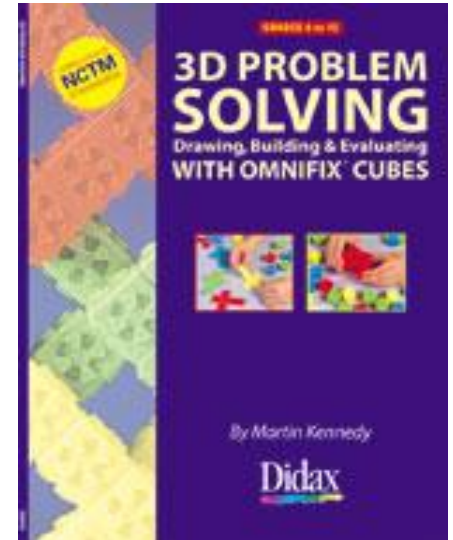
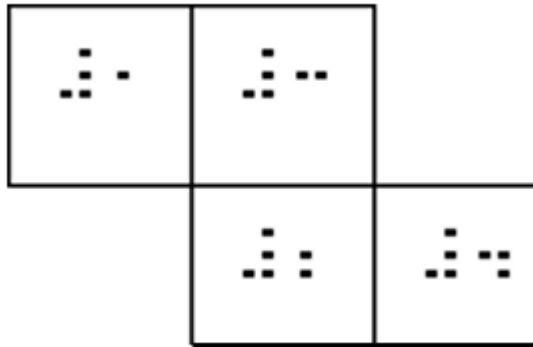
# Geometro GS10 Cylinder and Cone

- Provides students with flat plastic shapes (six circles, two rectangles, and two circle sectors) that can be readily joined to form two cylinders and two cones. Each have the same base, but different heights.



# Omnifix Cubes

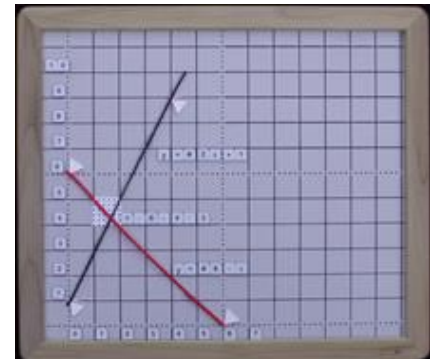
[www.didax.com](http://www.didax.com)



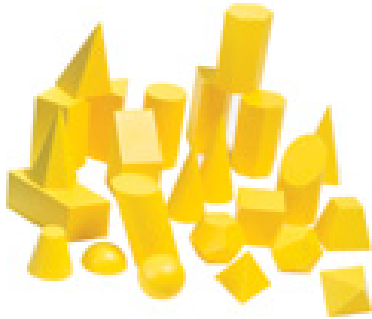


[www.mathwindow.com](http://www.mathwindow.com)

[www.mathwindow.com](http://www.mathwindow.com)



# Geometric Manipulatives



- Didax Plastic Geometric Models 25 shapes
- Discovery Toys Playful Patterns Design
- Didax 4 Geometric Templates



# Drawing/Construction Tools

- Drawing Board
- Compass

[www.maxiaids.com](http://www.maxiaids.com)

[www.fiskars.com](http://www.fiskars.com)

[www.APH.org](http://www.APH.org)

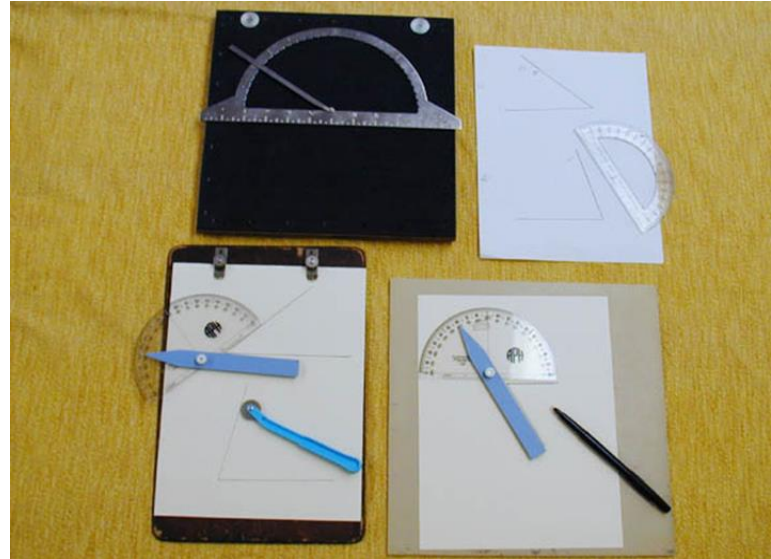
[www.staedtler.us/en/](http://www.staedtler.us/en/)

[www.easytactilegraphics.com/](http://www.easytactilegraphics.com/)



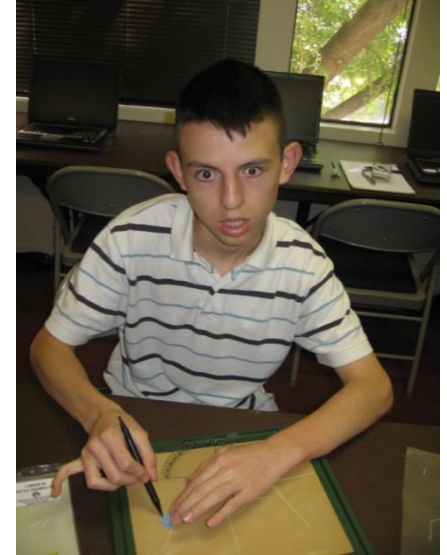
# Drawing/Construction Tools (cont.)

- Protractor
- Straightedge
- Tracing Wheel
- Stylus and/or Pen
- Drawing Board



[www.APH.org/](http://www.APH.org/)

# Students at Work Drawing



# Publications and Videos (Geometry)

- Geometric Constructions  
[www.tsbvi.edu/resources-math/3237-teaching-strategies#Geometric](http://www.tsbvi.edu/resources-math/3237-teaching-strategies#Geometric)  
[www.tsbvi.edu/videos-webinars/mathematics](http://www.tsbvi.edu/videos-webinars/mathematics)
- Transformations, Line Symmetry, and Tessellations  
[www.tsbvi.edu/resources-math/3237-teaching-strategies#Transformations](http://www.tsbvi.edu/resources-math/3237-teaching-strategies#Transformations)
- APH Braille/Print Protractor  
[www.tsbvi.edu/videos-webinars/mathematics](http://www.tsbvi.edu/videos-webinars/mathematics)

# New Geometry Videos

[www.tsbvi.edu/videos-webinars/mathematics](http://www.tsbvi.edu/videos-webinars/mathematics)

Videos for regular education math teachers that demonstrates teaching parallel lines, perpendicular lines, and skew lines to a student who is blind or visually impaired; strategies, tools, and materials.

- Parallel Lines
- Perpendicular Lines
- Skew Lines

# Other Math Resources

- Delta [www.delta-education.com](http://www.delta-education.com)
- Didax [www.didax.com](http://www.didax.com)
- ETA Hand2Mind [www.hand2mind.com](http://www.hand2mind.com)
- Math Forum [www.mathforum.org](http://www.mathforum.org)
- Nasco [www.enasco.com/math](http://www.enasco.com/math)
- Online Math Tutorial Videos  
[www.tsbvi.edu/videos-webinars/mathematics](http://www.tsbvi.edu/videos-webinars/mathematics)

Thank you for your kind attention.

Now, it's time for questions...